

# **Parameterization of non orographic gravity waves in large scale models**

## **Formalism, Impacts, and test against observations**

**François Lott,**

**LMD/IPSL/PSL (Ecole Normale Supérieure)-Paris**

- 1) Impact of gravity waves on the middle atmosphere climate
- 2) Spectral parameterizations and impact
- 3) Multiwave stochastic parameterizations  
and application to convective gravity waves
- 4) Application to gravity waves generated by fronts
- 5) Validation against balloon observations
- 6) Perspective

# Parameterization of GWs in large scale models

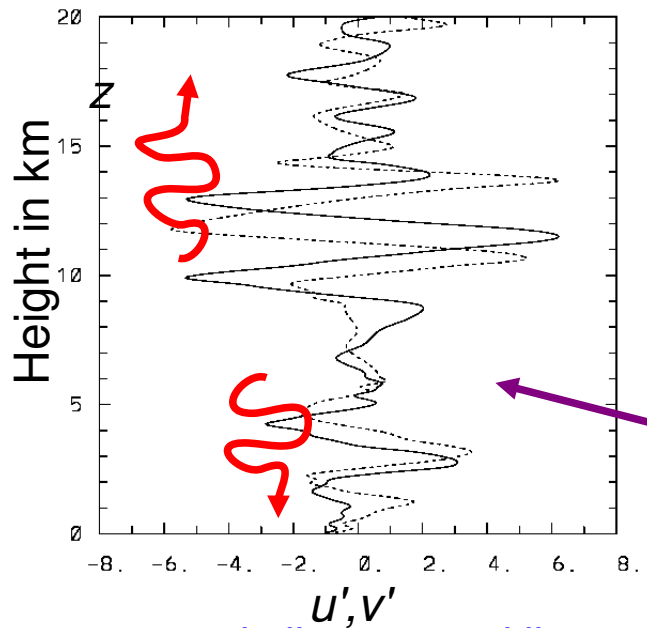
## 1) Impact of Gravity Waves on the middle atmosphere climate

Inertio internal gravity waves, intrinsic frequency :  $f < \Omega = \omega - \vec{k} \cdot \vec{U} < N$

### Source 1 (fronts):

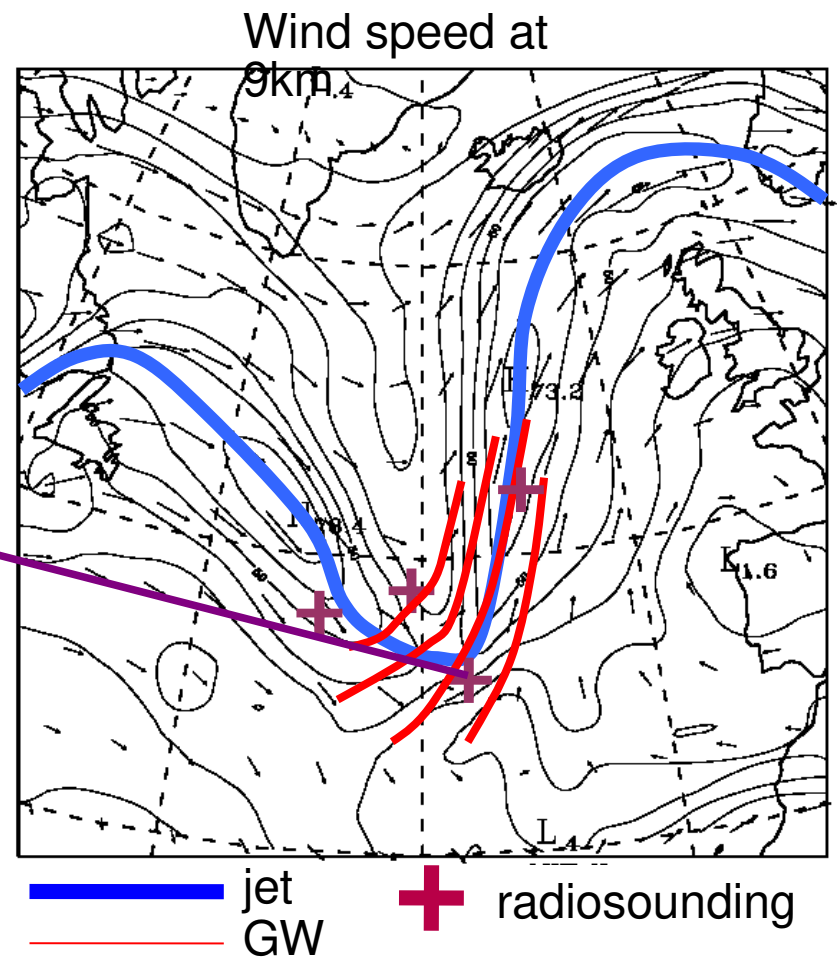
- Observation of a low frequency, large amplitude wave emitted in jet exit region (geostrophic adjustment?):

Vertical profile from a radiosounding



Plougonven, Teitelbaum & Zeitlin 03

$$\Omega \approx \pm f$$



— jet  
— GW  
+ radiosounding

# Parameterization of GWs in large scale models

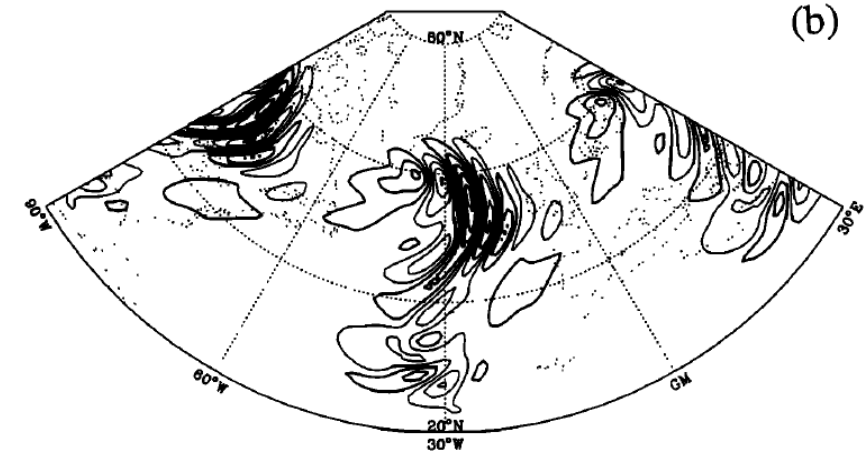
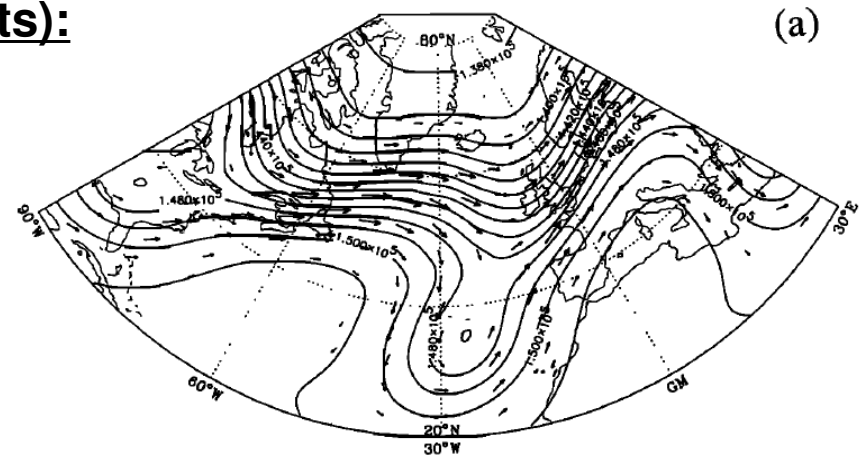
## 1) Impact of Gravity Waves on the middle atmosphere climate

Inertio internal gravity waves, intrinsic frequency :  $f < \Omega = \omega - \vec{k} \cdot \vec{U} < N$

### Source 1 (fronts):

Idealized numerical studies  
O'Sullivan and Dunkerton 1995

➔ Waves in Jet exit region



$$\Omega \approx \pm f$$

# Parameterization of GWs in large scale models

## 1) Impact of Gravity Waves on the middle atmosphere climate

Inertio internal gravity waves, intrinsic frequency :  $f < \Omega = \omega - \vec{k} \cdot \vec{U} < N$

### Source 2: Mountains

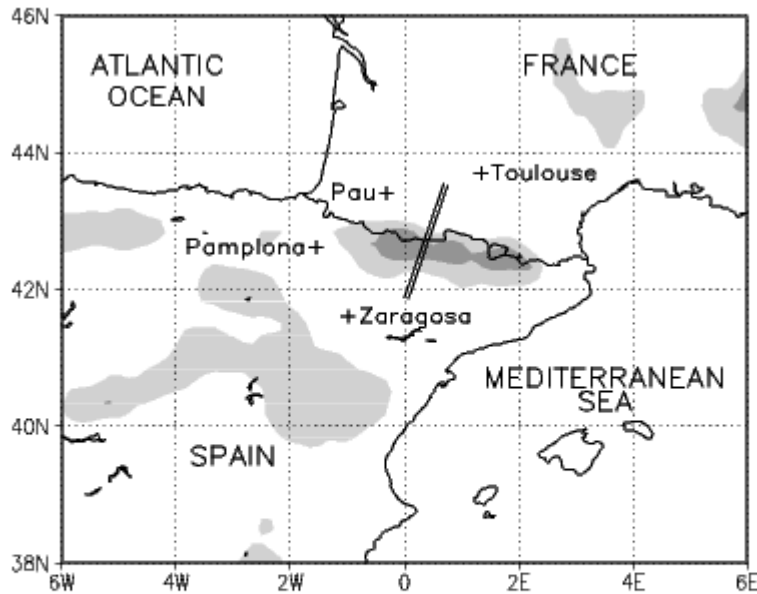


Figure 1: Smoothed terrain elevation and PYREX data used. + denotes the location of the high resolution soundings. The two thick lines indicate the airplane paths during the IOP 3. The light and dark shaded areas denote terrain elevation above 1000m and 1500m respectively.

$$\Omega \approx -\vec{k} \cdot \vec{U} < 0$$

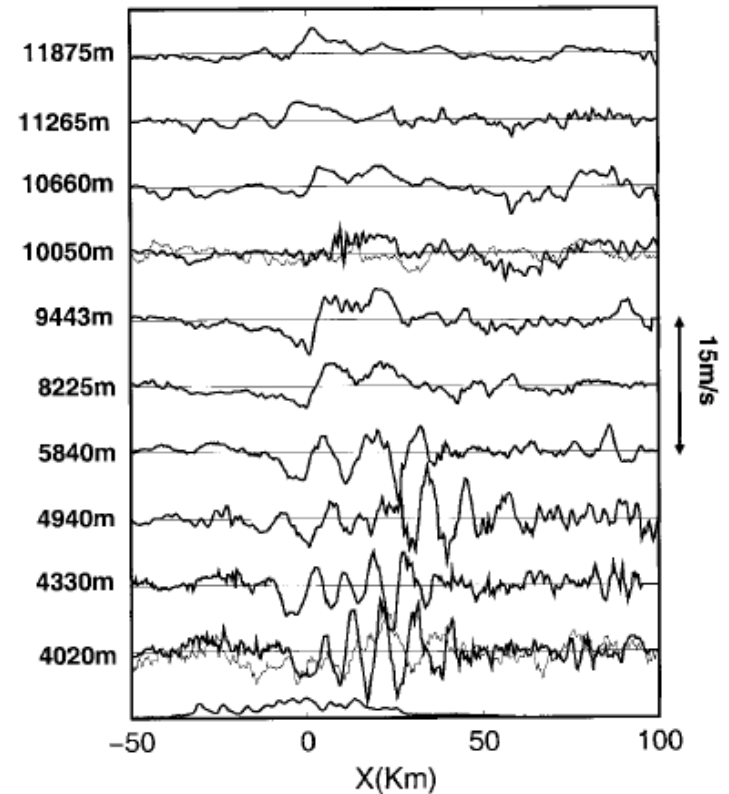


FIG. 2. Observed vertical velocities from different aircraft legs, from 15 Oct 1990 around 0600 UTC. Thick lower curve represents the Pyrenées; the thin curve at the  $Z = 4$  km and  $Z = 10$  km are red-noise surrogates with characteristics adapted to the measured vertical velocity at that level.

# Parameterization of GWs in large scale models

## 1) Impact of Gravity Waves on the middle atmosphere climate

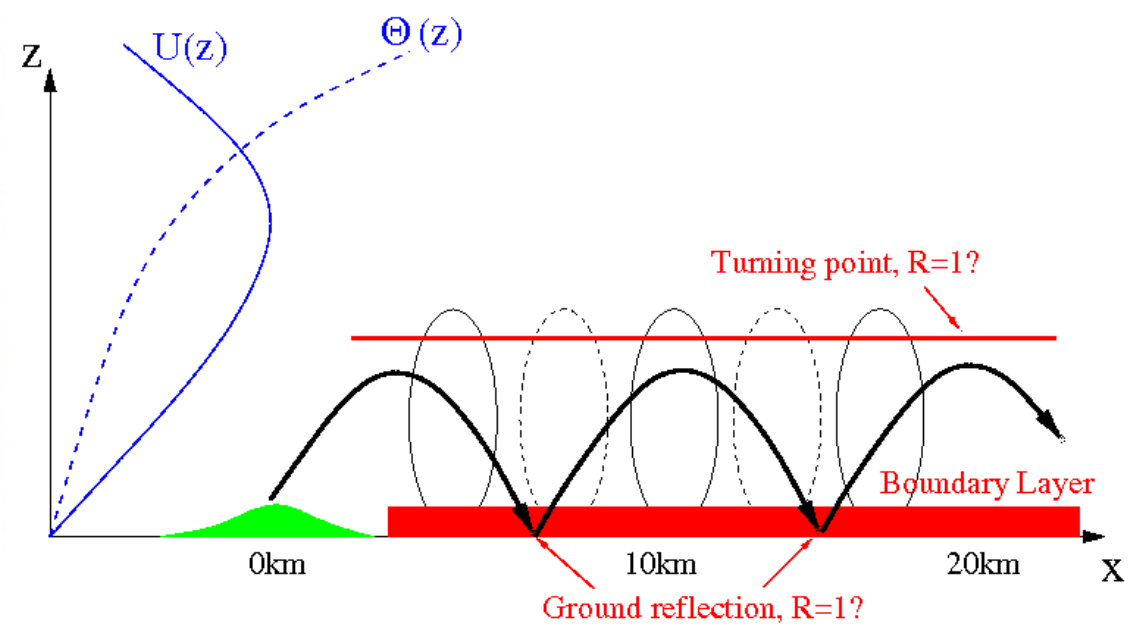
Inertio internal gravity waves, intrinsic frequency :  $f < \Omega = \omega - \vec{k} \cdot \vec{U} < N$

### Source 2: Mountains

Trapped lee-waves



Gravity waves trapping and lee waves (Scorer 1949)



$$\Omega \approx -\vec{k} \cdot \vec{U} < 0$$

# Parameterization of GWs in large scale models

## 1) Impact of Gravity Waves on the middle atmosphere climate

Inertio internal gravity waves, intrinsic frequency :  $f < \Omega = \omega - \vec{k} \cdot \vec{U} < N$

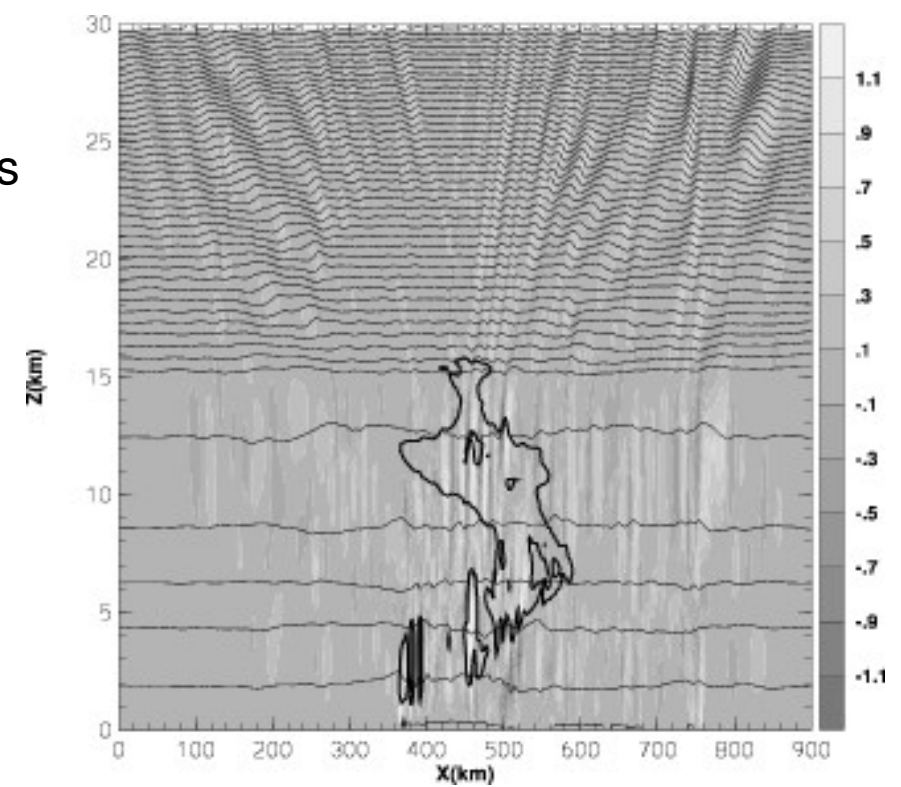
### Source 3: Convection

The heating produce waves in both directions of propagation

$$\Omega > 0 \text{ and } \Omega < 0$$

### Sources 1, 2, and 3 :

All these waves have horizontal scale much smaller than the scales resolved by climate models (still today !), they need to be parameterized



Gravity waves above a convective cloud (Alexander et Holton 1997)



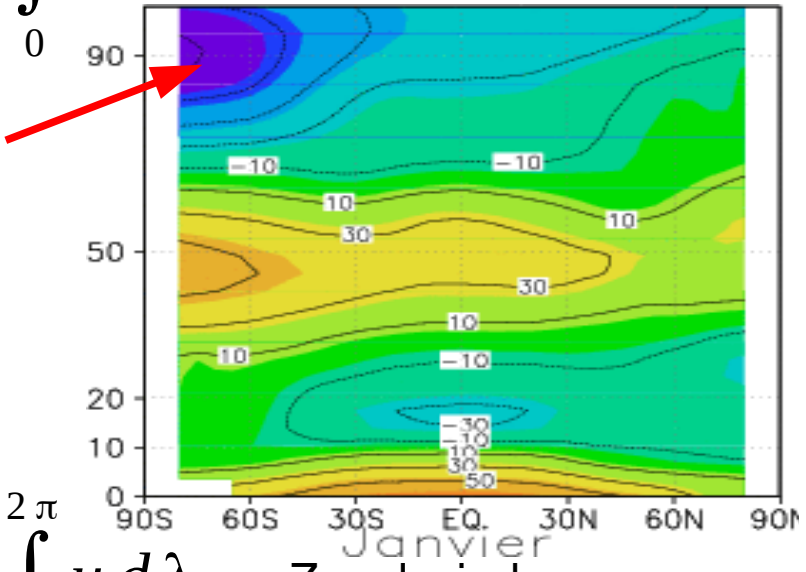
# Parameterization of GWs in large scale models

## 1) Impact of Gravity Waves on the middle atmosphere climate

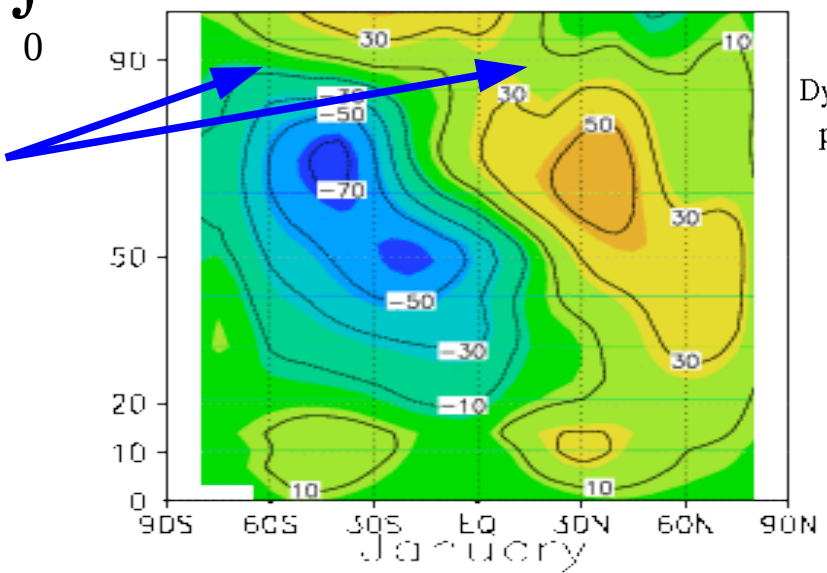
Midlatitudes. minima of T at the summer pole near the mesopause

Closure of the midlatitude jets

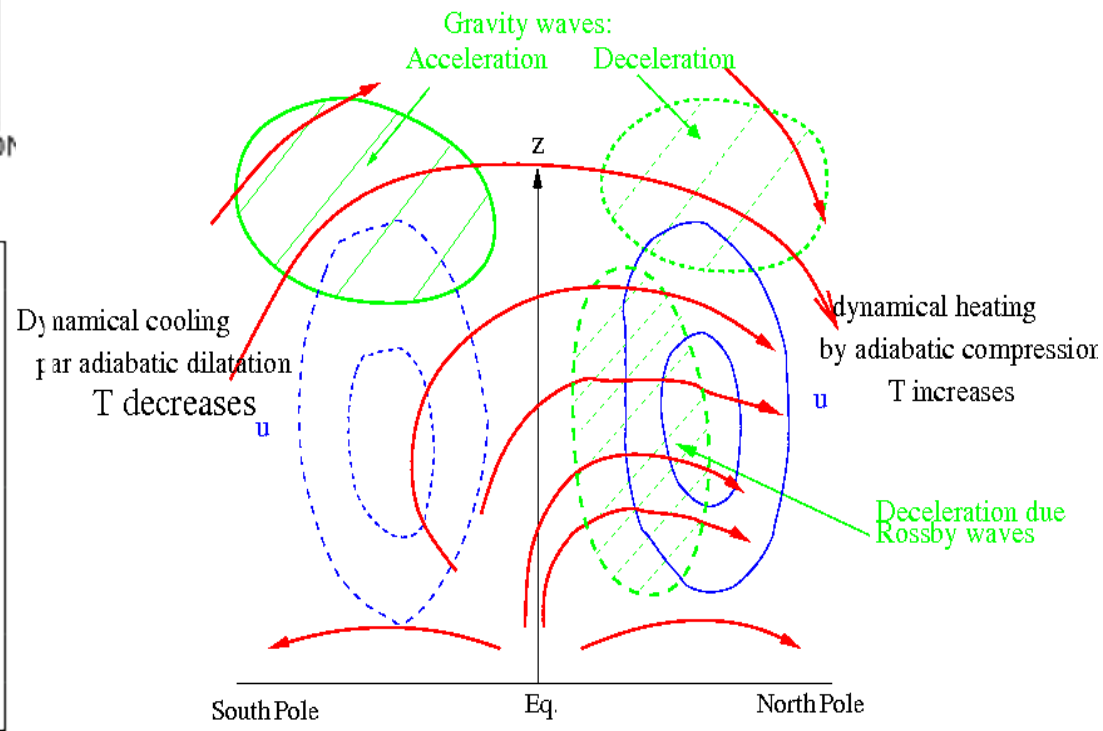
$$\bar{T} = \frac{1}{2\pi} \int_0^{2\pi} T d\lambda$$



$$\bar{u} = \frac{1}{2\pi} \int_0^{2\pi} u d\lambda$$



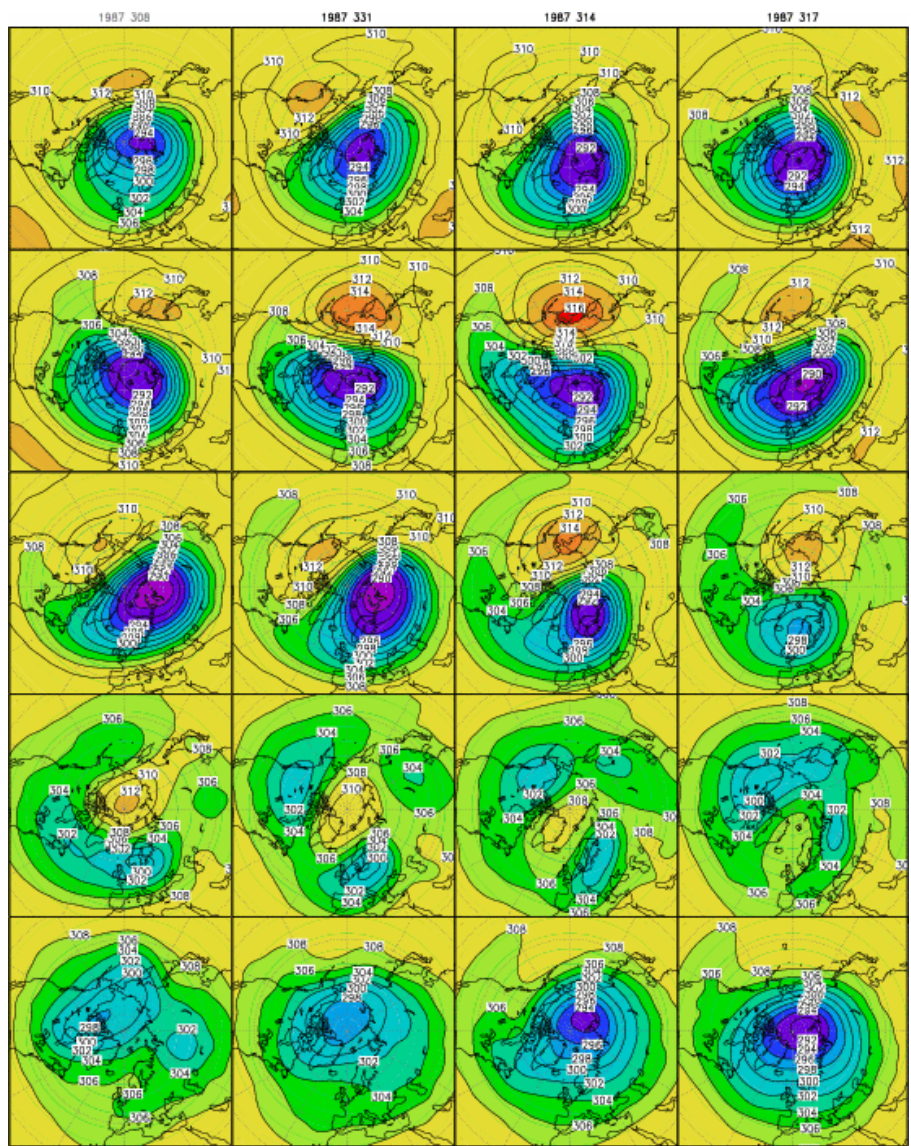
The meridional circulation driven by waves and the « downward control »  
(review in Haynes et al. ~1991)



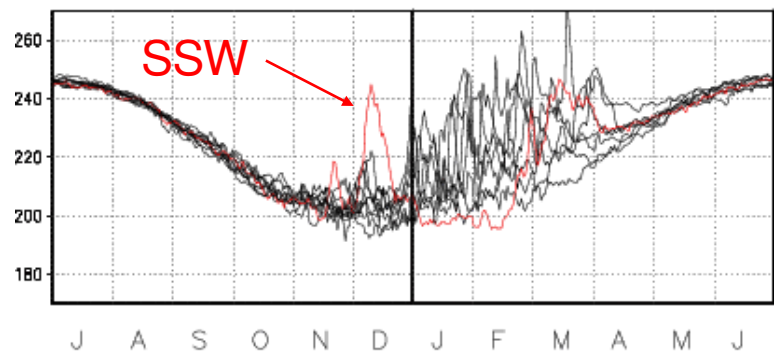
# Parameterization of GWs in large scale models

## 1) Impact of Gravity Waves on the middle atmosphere climate

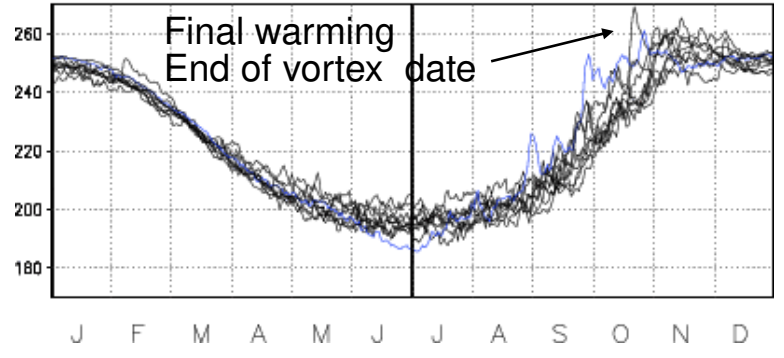
**The gravity waves are not alone:** planetary scale Rossby waves also provide a large Deceleration in the middle atmosphere, here Z at around 32km every 3 days in 1987-1988 early winter, and when occur Sudden Stratospheric Warmings



Temperature at the North pole, z=32km



Temperature at the South poles, z=32km



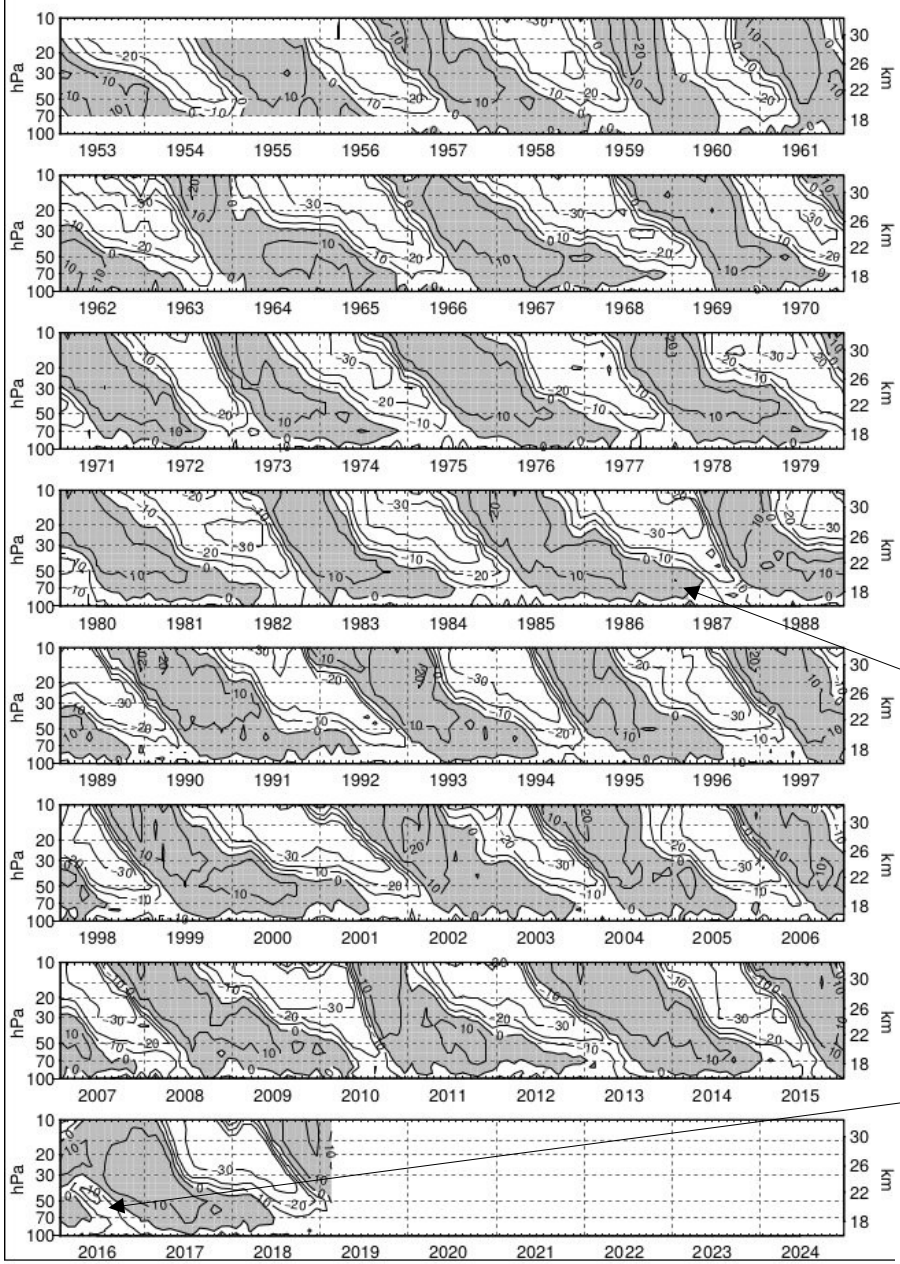
Vertical Structure Equation for Rossby waves

$$\hat{\Phi}_{zz} + \left( \frac{N^2}{f^2} \left( \frac{\beta}{\bar{u}_0} - k^2 - l^2 \right) - \frac{1}{4H^2} \right) \hat{\Phi} = 0$$



# Parameterization of GWs in large scale models

## 1) Impact of Gravity Waves on the middle atmosphere climate



**Tropics : Quasi biennial oscillation**  
of the zonal mean zonal wind at  
the equator,  
 $\bar{u}(t, 0, z)$

Radiosonde observations at Singapour  
since 1952

Aperiodic decent of zonal mean zonal  
Winds  
(mean period 27.5 month)

Stalling of the westerlies near  
above the tropopause

Not well reproduce in models around  
100hPa

Recent disruptions that may  
be caused by the changing  
climate

See QBO Initiative  
Butchart et al. (GMD 2017)

# Parameterization of GWs in large scale models

## 1) Impact of Gravity Waves on the middle atmosphere climate

Plumb (1977)'s model with 2 GWs interacting with the zonal wind:

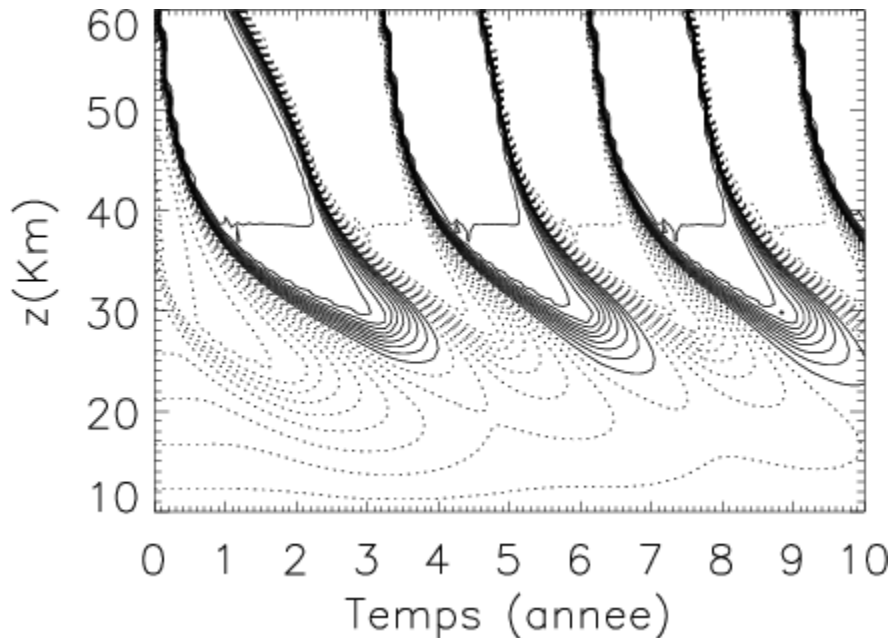
$$\frac{\partial \bar{u}}{\partial t} = \sum_{i=1}^2 \frac{\partial \bar{F}_i^z}{\partial z} + \nu \frac{\partial^2 \bar{u}}{\partial z^2}$$

$\bar{F}$  momentum flux of a single wave  
(planetary or gravity)  
(explicit or parameterized)

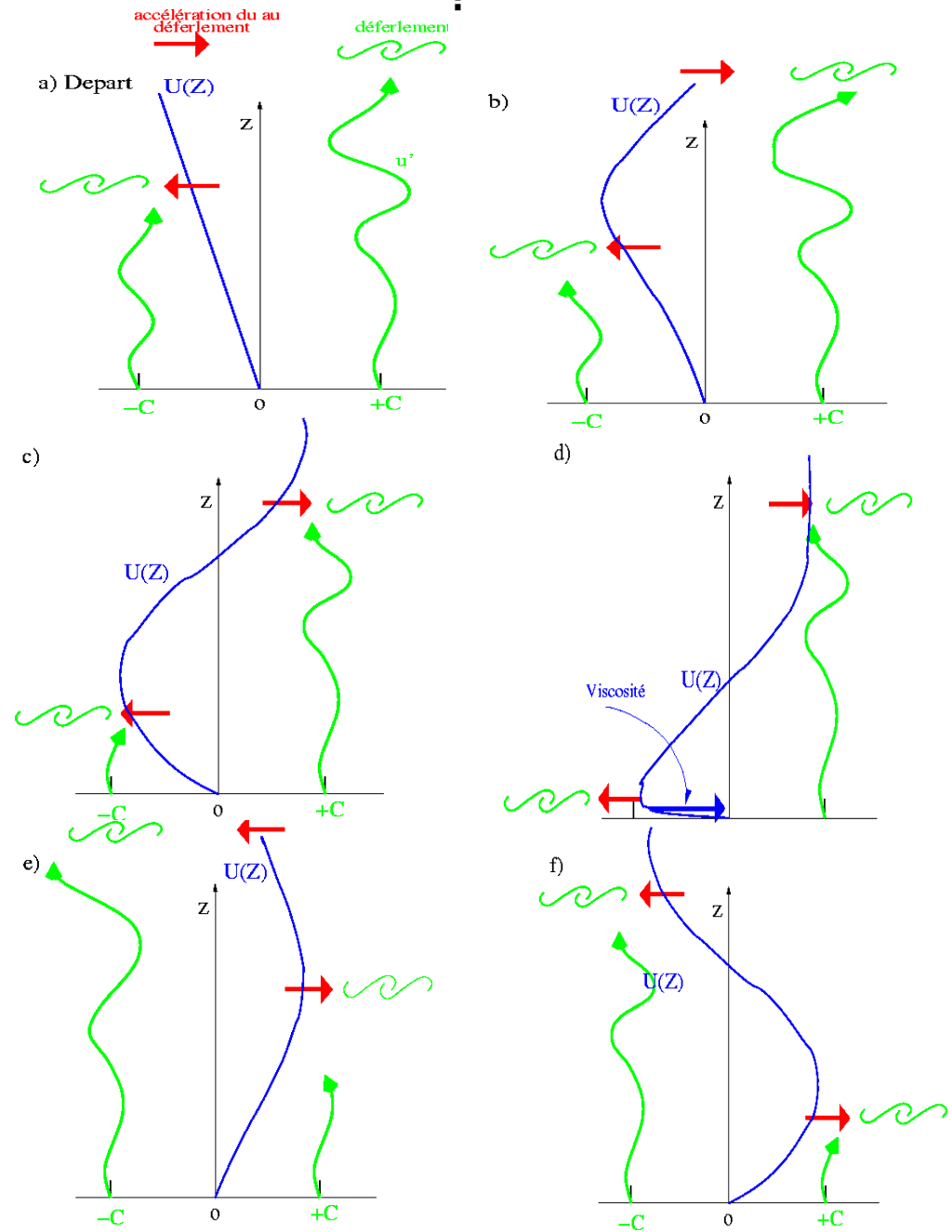
$$\bar{F}_i = \overline{\rho u_i' w_i'}$$

Result from the theoretical model:

$$\bar{u}(z, t)$$



### Interpretation:

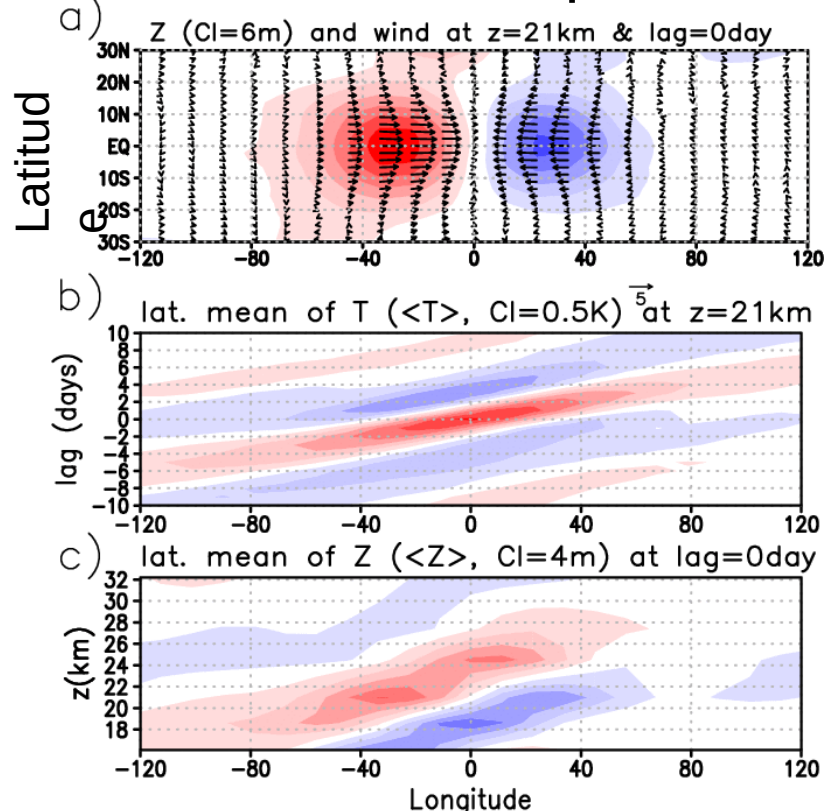


# Parameterization of GWs in large scale models

## 1) Impact of Gravity Waves on the middle atmosphere climate

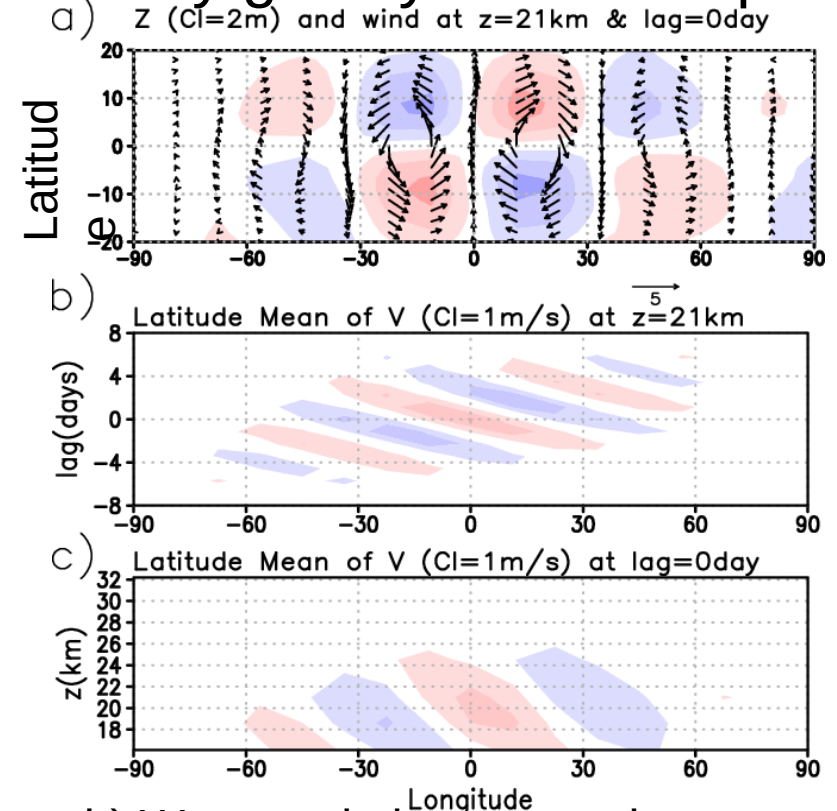
The gravity waves are not alone !

### Kelvin wave composites



- a) Pressure and wind structure at 21 km
- b) Eastward propagation
- c) Phase lines inclined eastward with altitude: upward propagation

### Rossby gravity wave composites



- b) Westward phase speed eastward group speed
- c) Phase lines inclined westward with altitude : upward propagation

Extraction of equatorial waves in reanalysis (for instance MERRA) and models :  
 Lott Kuttipurath and Vial (JAS 2007) ; Lott et al.~(JGR 2014) ; Holt Lott et al. (QJRMS 2021)

# Parameterization of GWs in large scale models

## 2) Spectral parameterization and impact

Subgrid scale parametrizations are based on Fourier series decomposition of the waves field over the model gridbox of sizes  $\delta x$ ,  $\delta y$ , and  $\delta t$  ( $\delta t$  can be larger than the model time-step).

$$w' = \sum_a \sum_b \sum_c \hat{w}(k_a, l_b, \omega_c) e^{i(k_a x + l_b y - \omega_c t)} \quad \text{a, b, c are integers, and } k_a = a \frac{2\pi}{\delta x}, l_b = b \frac{2\pi}{\delta y}, \omega_c = c \frac{2\pi}{\delta t}$$

(dropped in the following)

Since a lot of waves with different characteristics are needed this triple Fourier series can be very expensive to evaluate each timestep

### Multiwaves schemes:

Garcia et al. (2007),  
Alexander and Dunkerton (1999)  
Treat the large ensemble of waves but each quite independently from the others and using Lindzen (1981) to evaluate the breaking.

### Globally spectral schemes:

Treat the spectra globally, and using analytical integrals of its different parts

Hine (1997),  
Manzini and McFarlane (1997)

Warner and McIntyre (2001)



# Parameterization of GWs in large scale models

## 2) Spectral parametrizations and impact

### Globally spectral schemes,

Use that the observed GWs vertical (m-)spectra have a quasi-universal shape, with a  $m^{-3}$  slope for the  $m > m^*$  part of the spectra that correspond to breaking waves

The **Warner and McIntyre (2001)** scheme propagate initial gravity wave spectra according to wave action conservation rules and truncate the propagated when it exceeds the  $m^{-3}$  saturated spectra to fit observed spectra

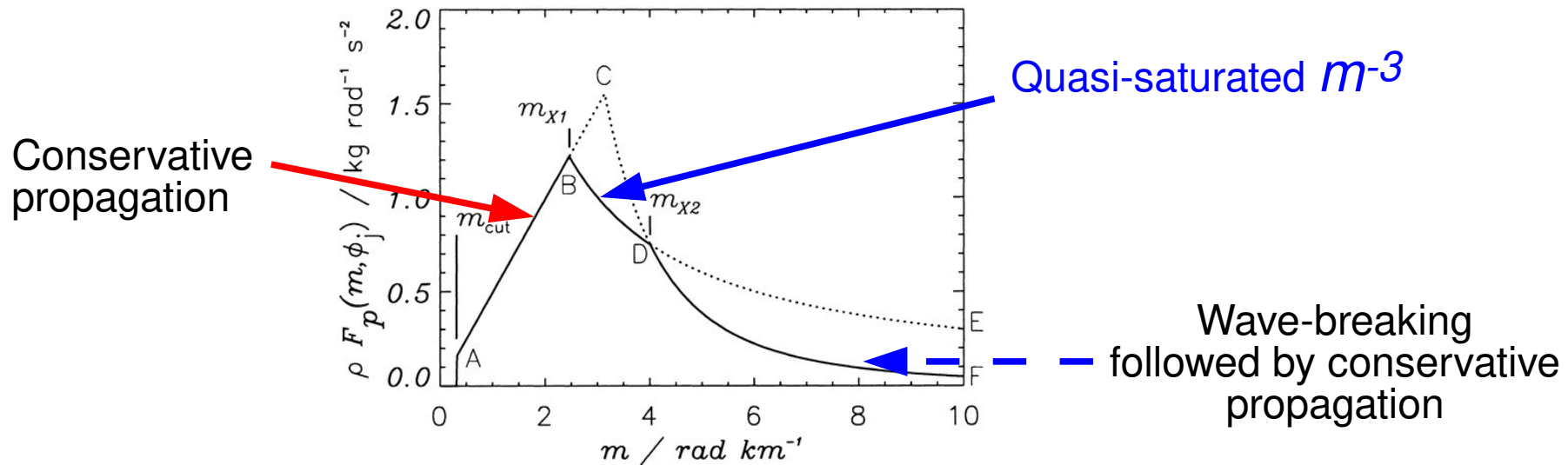


Fig. 1, from Warner and McIntyre (2001)



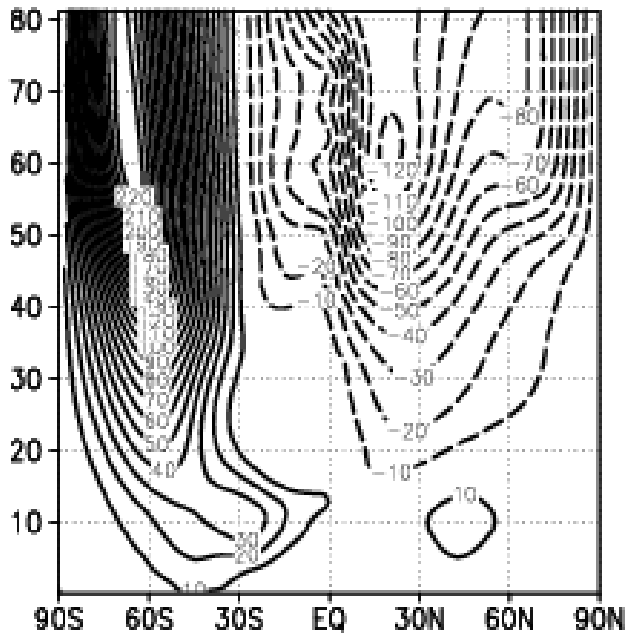
# Parameterization of GWs in large scale models

## 2) Spectral parametrizations and impact

The effect of gravity waves can be well seen in the mesosphere if we compare simulations with and without parameterization LMDz (Lott et al. 2005, Lott and Millet 2010).

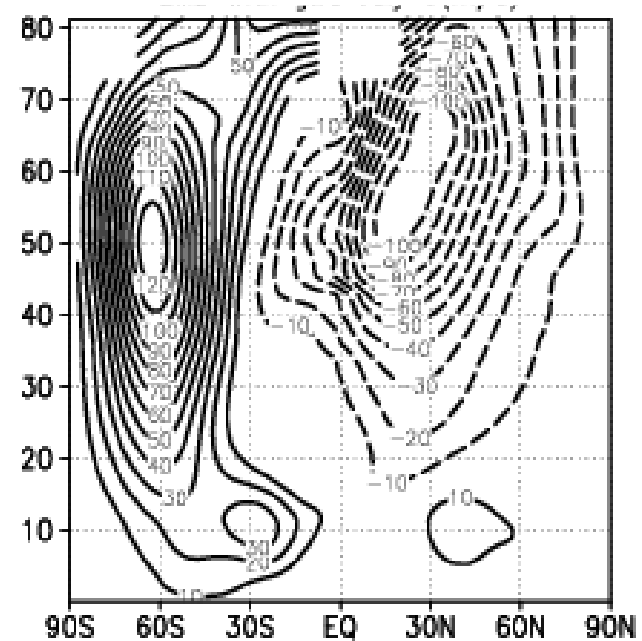
Here are used the Hines' scheme developed by Manzini et al.(1997) and the Lott and Miller (1997) orographic scheme.

without  
**July**



$$\bar{u} = \frac{1}{2\pi} \int_0^{2\pi} u d\lambda$$

with  
**July**



# Parameterization of GWs in large scale models

## 2) Spectral parametrizations and impact

The effect of gravity waves can be well seen in the mesosphere if we compare simulations with and without parameterization LMDz (Lott et al. 2005, Lott and Millet 2010).

Here are used the Hines' scheme developed by Manzini et al.(1997) and the Lott and Miller (1997) orographic scheme.

$$\bar{u} = \frac{1}{2\pi} \int_0^{2\pi} u d\lambda$$

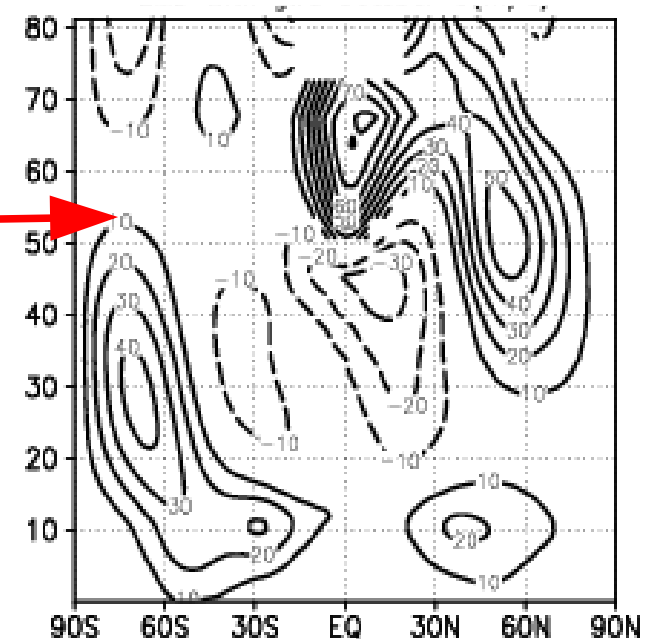
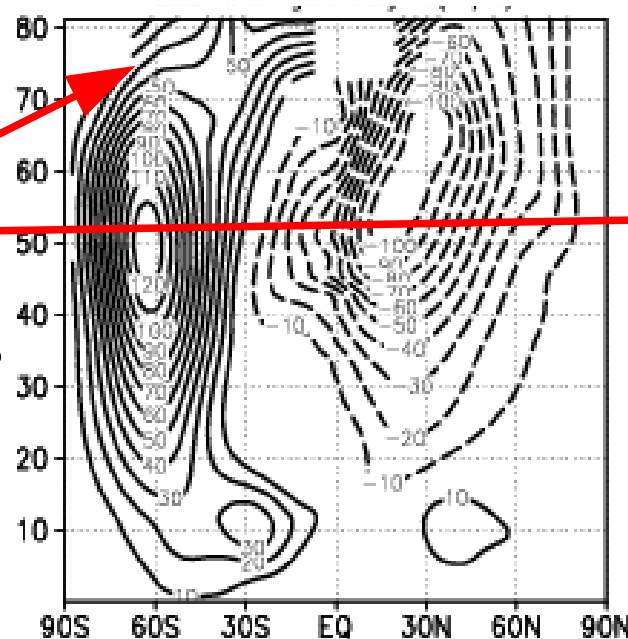
July

October

Descend of the  
 $\bar{u} = 0$   
Line.

Date when it arrives  
At 10hPa :  
Final warming

**Systematic Error !**



## Parameterization of GWs in large scale models

### 3) Multiwave stochastic param. and application to convective GWs

Exemple of the stochastic and « Multiwave » convective gravity wave scheme used in LMDz6 / IPSLCM6 model [Lott Guez and Maury GRL, 2012, Lott and Guez 2013]

**Stochastic series** with intermittency coefficients  $A_n$ 's :

$$w' = \sum_{n=1}^{\infty} A_n \hat{w}_n(z) e^{z/2H} e^{i(k_n(x - C_n t))} \quad \sum_{n=1}^{\infty} A_n^2 = 1$$

$k_n, c_n$  chosen randomly, tunable parameter :  $C_0$  characteristic intrinsic phase speed

**Launched flux :**

$$\rho \hat{w}_n \hat{u}_n^*(z_l) \approx \rho_r \frac{k_n}{|\vec{k}_n|} \exp(-m_{nl}^2 \Delta z^2) G_{uw} P_r^2$$

Pr : gridscale precipitation

$\Delta z$  : Source depth

$G_{uw}$  : amplitude parameter

$Z_l$  : Launching altitude

**Saturation criteria** (dynamical filtering):

$$|\rho \hat{w}_n \hat{u}_n^*| \leq \rho_r S_c^2 |c_n - U(z)|^3 \frac{k_m}{N |k_n|^3}$$

$S_c$  : Saturation parameter

# Parameterization of GWs in large scale models

## 3) Multiwave stochastic param. and application to convective GWs

### Online results with LMDz

LMDz version with 80 levels,  $dz < 1\text{km}$   
In the stratosphere

QBO of irregular  
period with mean  
around 26month,

20% too small amplitude

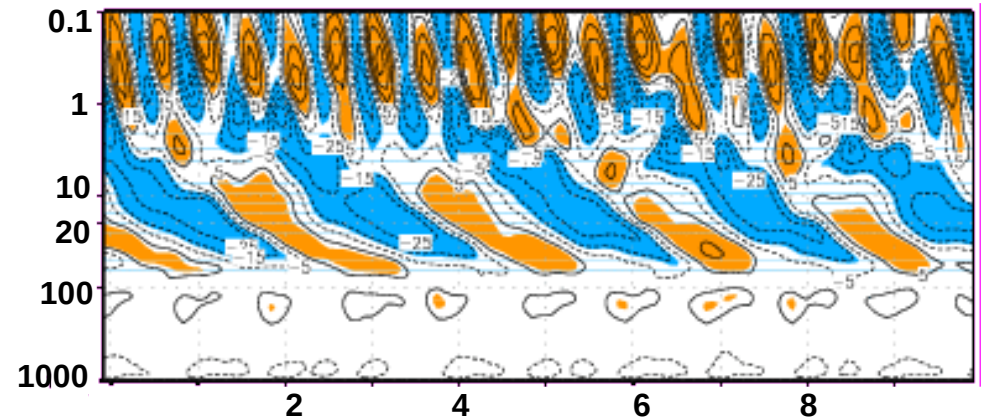
#### **Systematic Error :**

To small amplitude westerlies near  
Above 100hPa

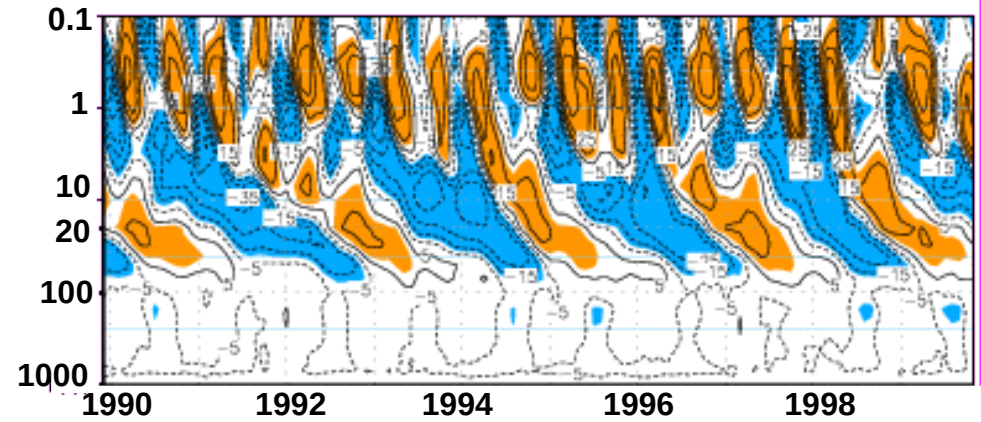
(Problem : this is probably the altitude  
At which the QBO correlated with  
the midlatitudes

(Anstey et al. 2021,  
The Holton-Tan (1980) effect)

a) LMDz with convective GWs **LMDz+CGWs**



b) MERRA



Lott and Guez, JGR13

# Parameterization of GWs in large scale models

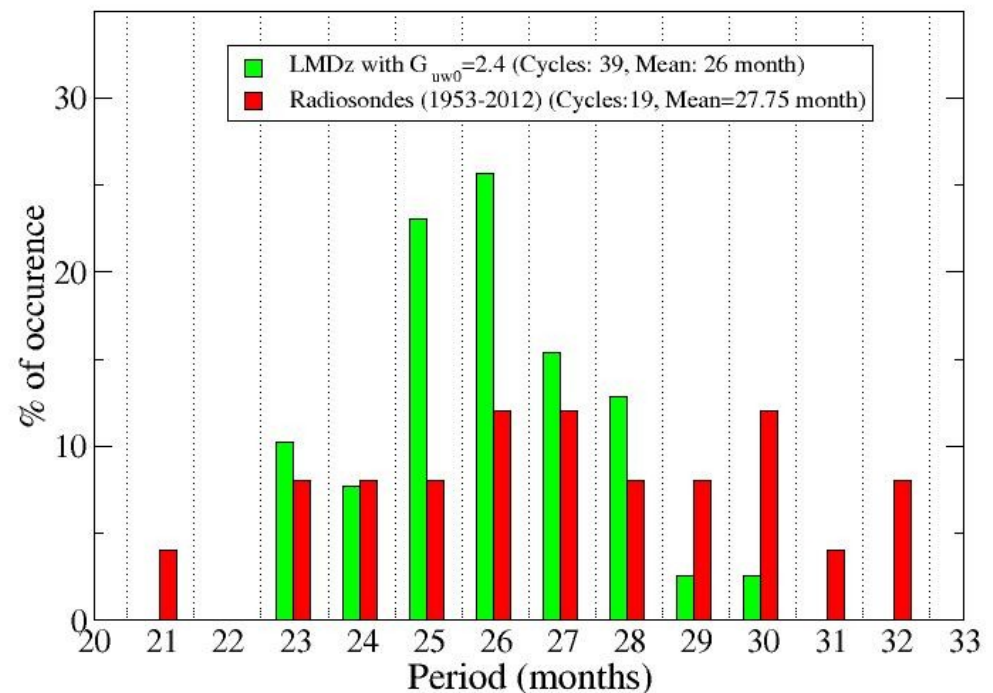
## 3) Multiwave stochastic param. and application to convective GWs

### Online results with LMDz

#### Histogram of QBO periods

Relatively good spread of the periods taking into account that it is a forced simulation with climatological SST (no ENSO)

Periods related to the annual cycle (multiples of 6 months) are not favoured probably related to the weak relations with the SAO





# Parameterization of GWs in large scale models

## 3) Multiwave stochastic param. and application to convective GWs

### Equatorial waves:

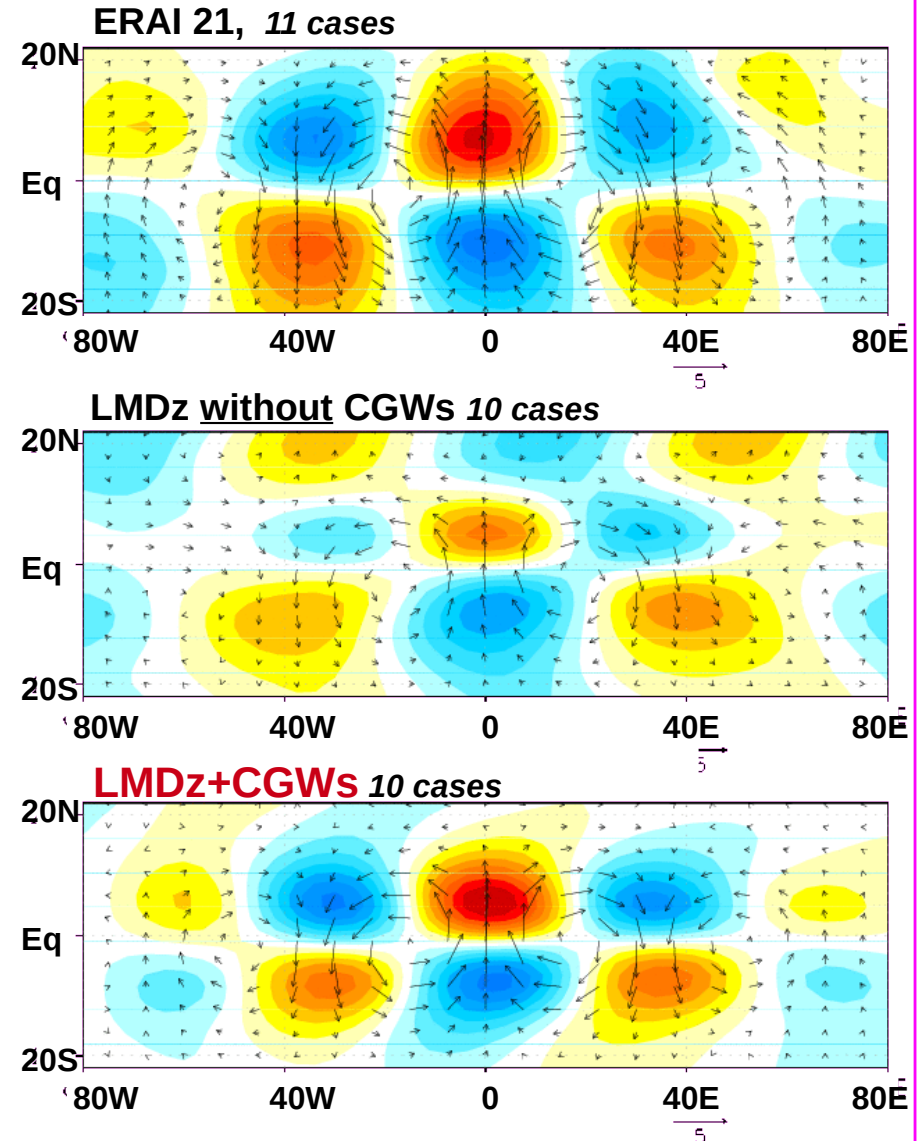
Remember also that when you start to have positive zonal winds, **the planetary scale Yanai wave is much improved**

*(the composite method is described in Lott et al. 2009)*

**Zero longitude line arbitrary**

*Lott et al. 2012 GRL*

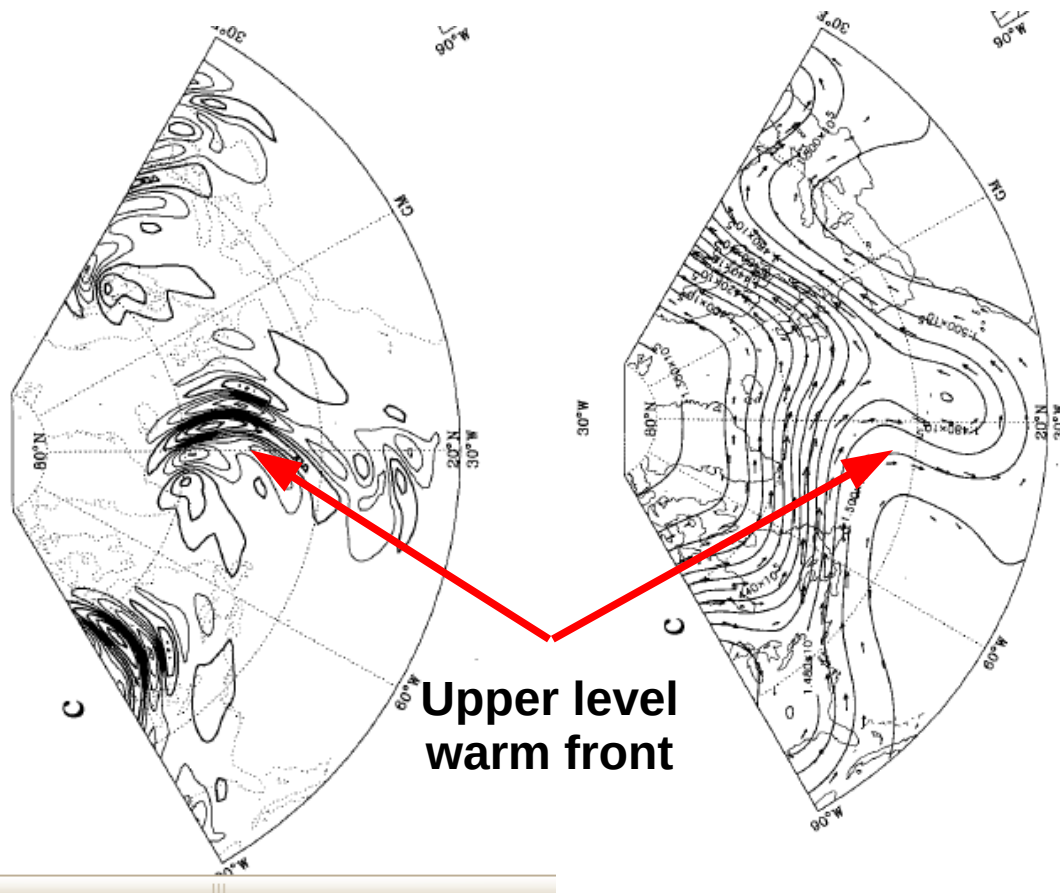
### Composite of Rossby-gravity waves with $s=4-8$ Temp (CI=0.1K) and Wind at 50hPa & lag = 0day



# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Simulations to support these parameterizations:



O'Sullivan and Dunkerton (1995)

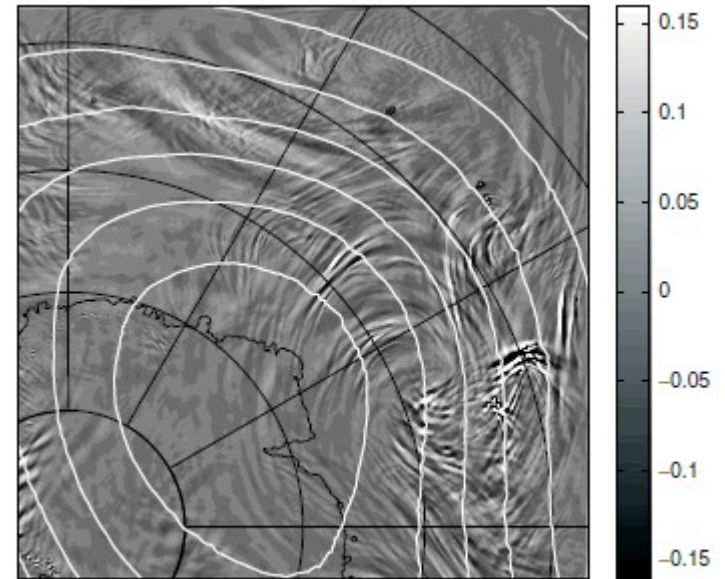


Figure 16. As Figure 2(b), but from a simulation with doubled horizontal resolution ( $\Delta x = 10$  km).

Results confirmed by much higher resolution simulations

Plougonven Hertzog and Guez (2012)

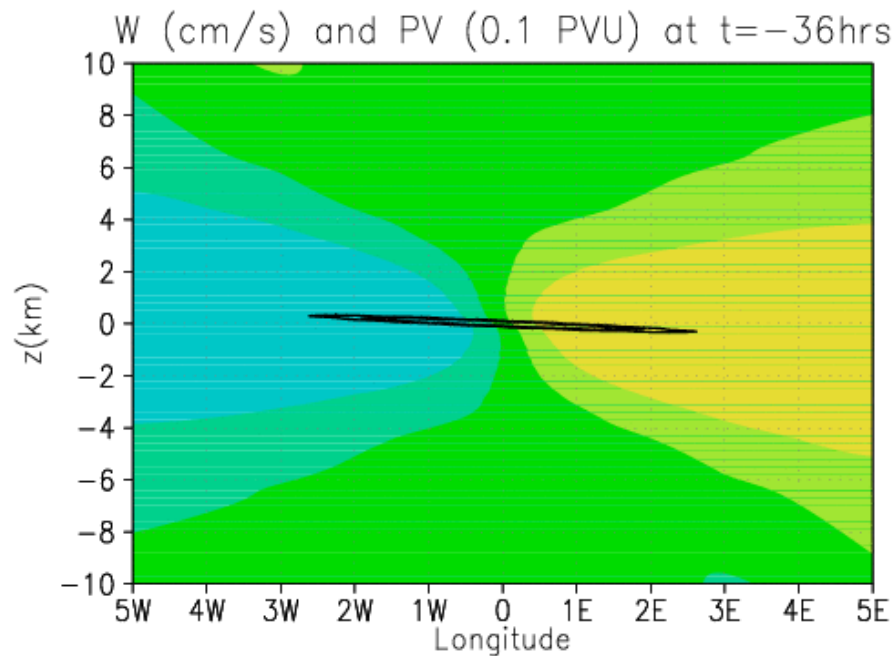
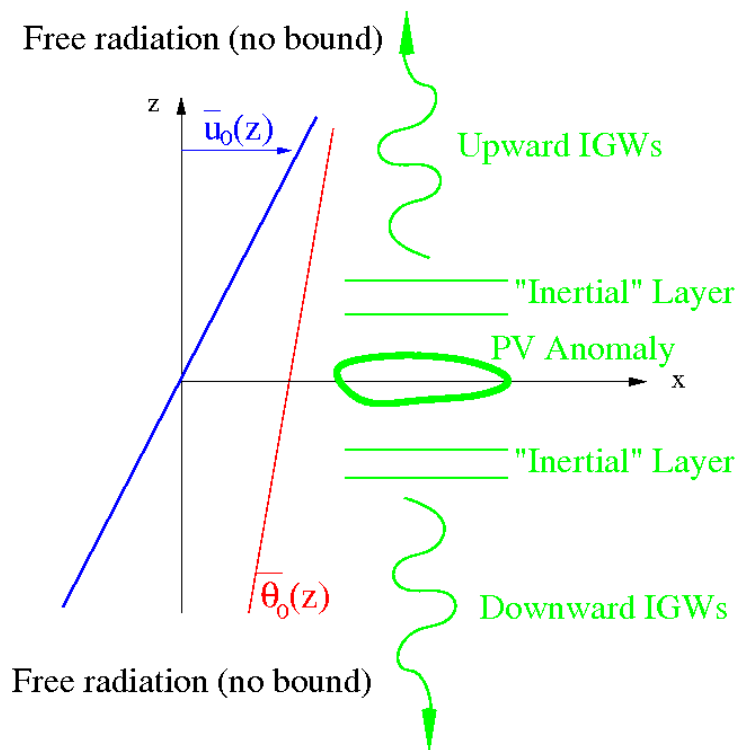
This is somehow related to the “Geostrophic Adjustment” process.  
Part of it, the so-called «Spontaneous adjustment» where a well-balanced flow radiates GWs can be handled analytically  
Lott, Plougonven, Vanneste (2010, 2012)

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Well balanced means entirely described by the Potential vorticity distribution:

Spontaneous emission : GW emission from 3D (x,y,z) Potential Vorticity (PV) anomaly advected in a rotating ( $f = cte$ ), stratified ( $N = cte$ ) shear flow (vertical shear  $\Lambda = \bar{u}_{0z} = cte$ ).



Underlying justification : fronts are characterized by strong PV anomalies and wind shears

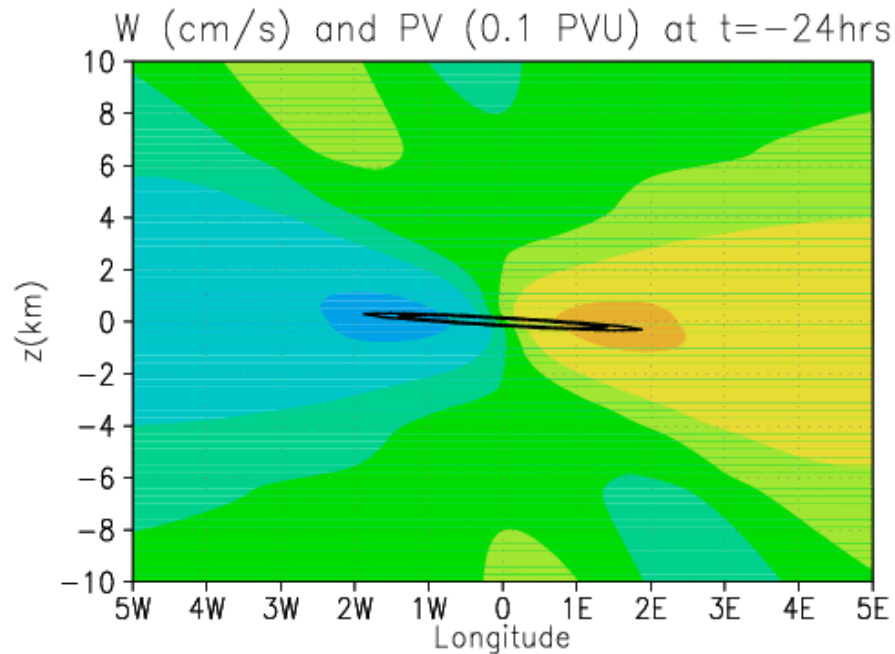
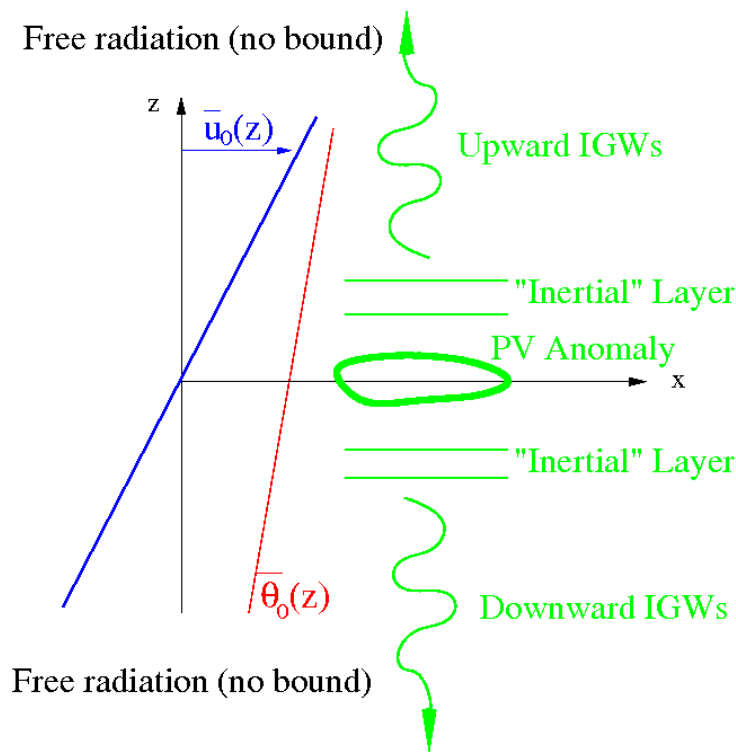
*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Well balanced means entirely described by the Potential vorticity distribution:

Spontaneous emission : GW emission from 3D (x,y,z) Potential Vorticity (PV) anomaly advected in a rotating ( $f = cte$ ), stratified ( $N = cte$ ) shear flow (vertical shear  $\Lambda = \bar{u}_{0z} = cte$ ).



Underlying justification : fronts are characterized by strong PV anomalies and wind shears

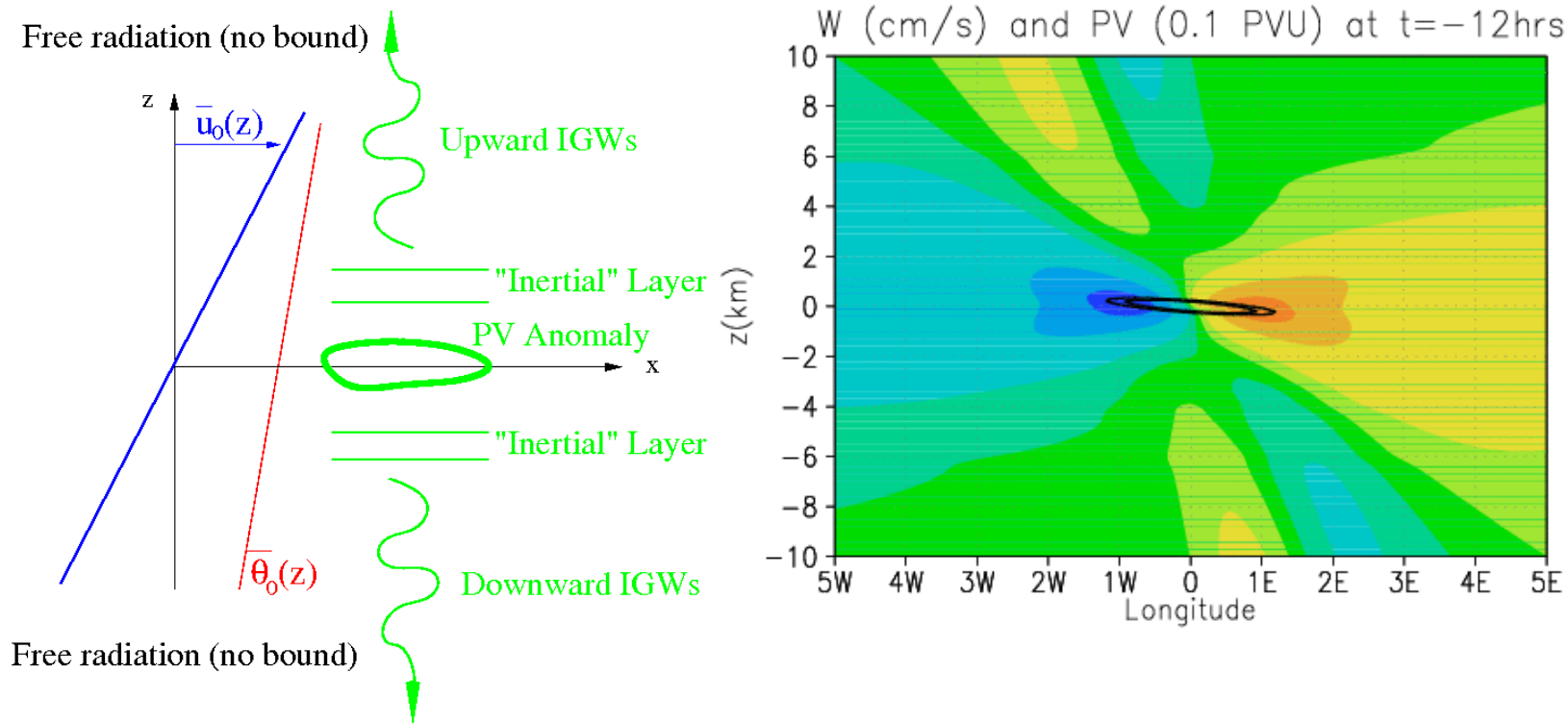
*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Well balanced means entirely described by the Potential vorticity distribution:

Spontaneous emission : GW emission from 3D (x,y,z) Potential Vorticity (PV) anomaly advected in a rotating ( $f = cte$ ), stratified ( $N = cte$ ) shear flow (vertical shear  $\Lambda = \bar{u}_{0z} = cte$ ).



Underlying justification : fronts are characterized by strong PV anomalies and wind shears

*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

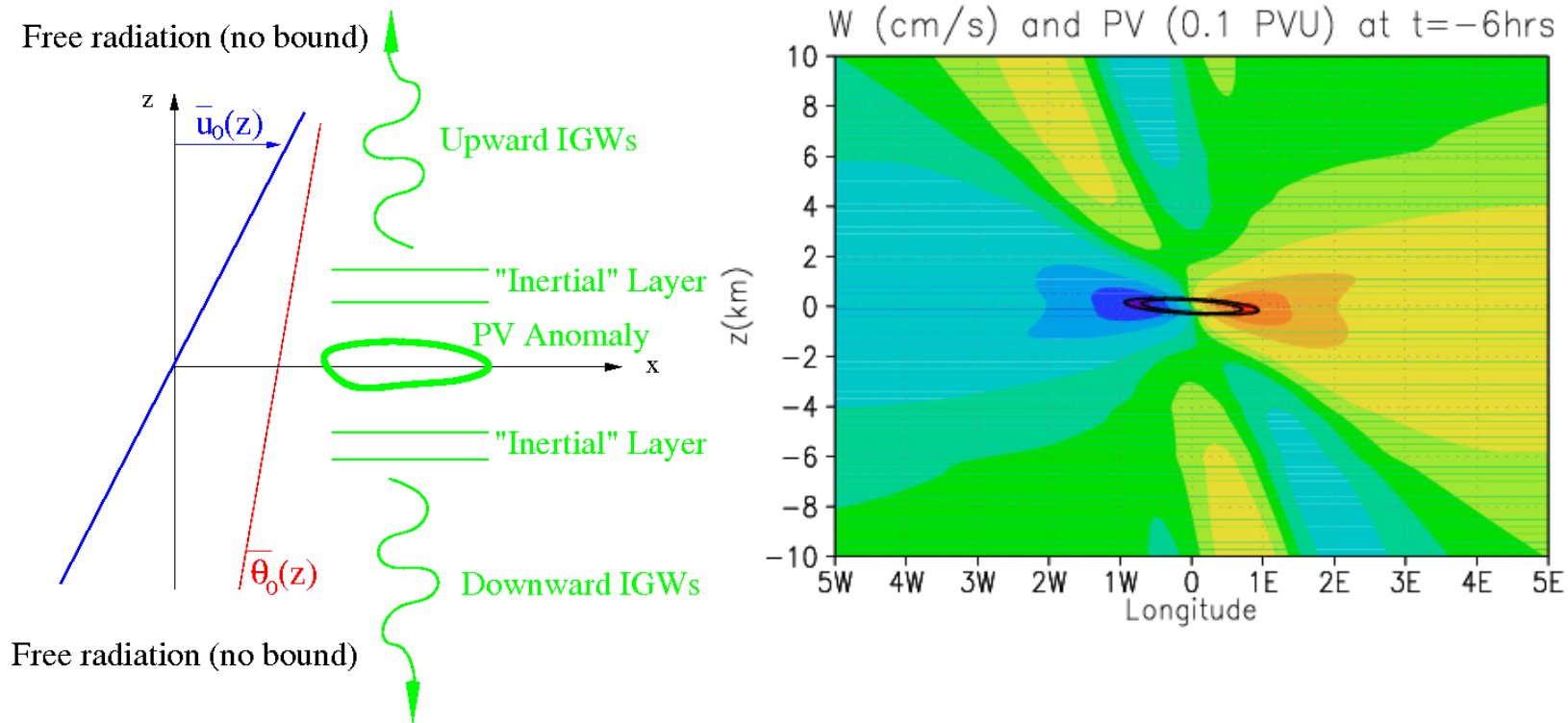


# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Well balanced means entirely described by the Potential vorticity distribution:

Spontaneous emission : GW emission from 3D (x,y,z) Potential Vorticity (PV) anomaly advected in a rotating ( $f = cte$ ), stratified ( $N = cte$ ) shear flow (vertical shear  $\Lambda = \bar{u}_{0z} = cte$ ).



Underlying justification : fronts are characterized by strong PV anomalies and wind shears

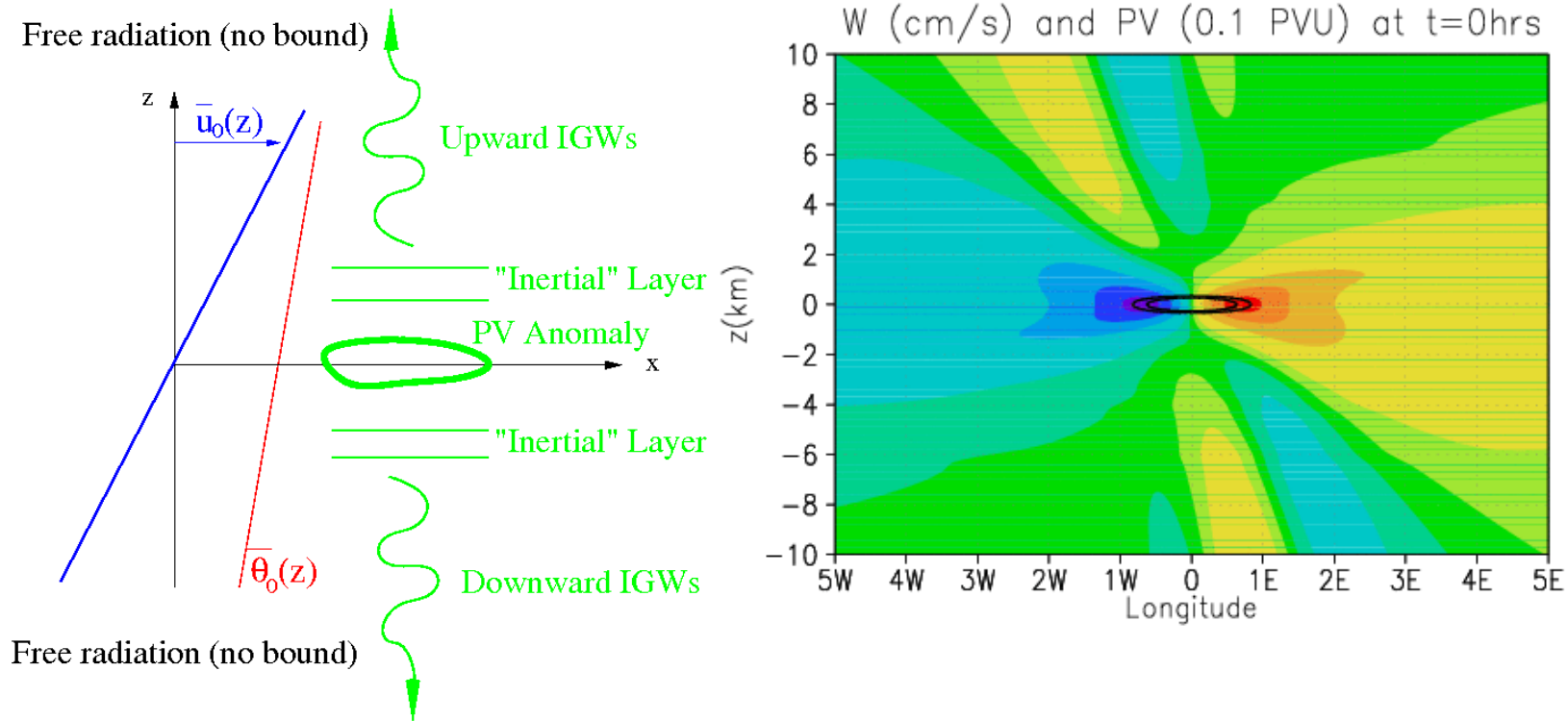
*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Well balanced means entirely described by the Potential vorticity distribution:

Spontaneous emission : GW emission from 3D (x,y,z) Potential Vorticity (PV) anomaly advected in a rotating ( $f = cte$ ), stratified ( $N = cte$ ) shear flow (vertical shear  $\Lambda = \bar{u}_{0z} = cte$ ).



Underlying justification : fronts are characterized by strong PV anomalies and wind shears

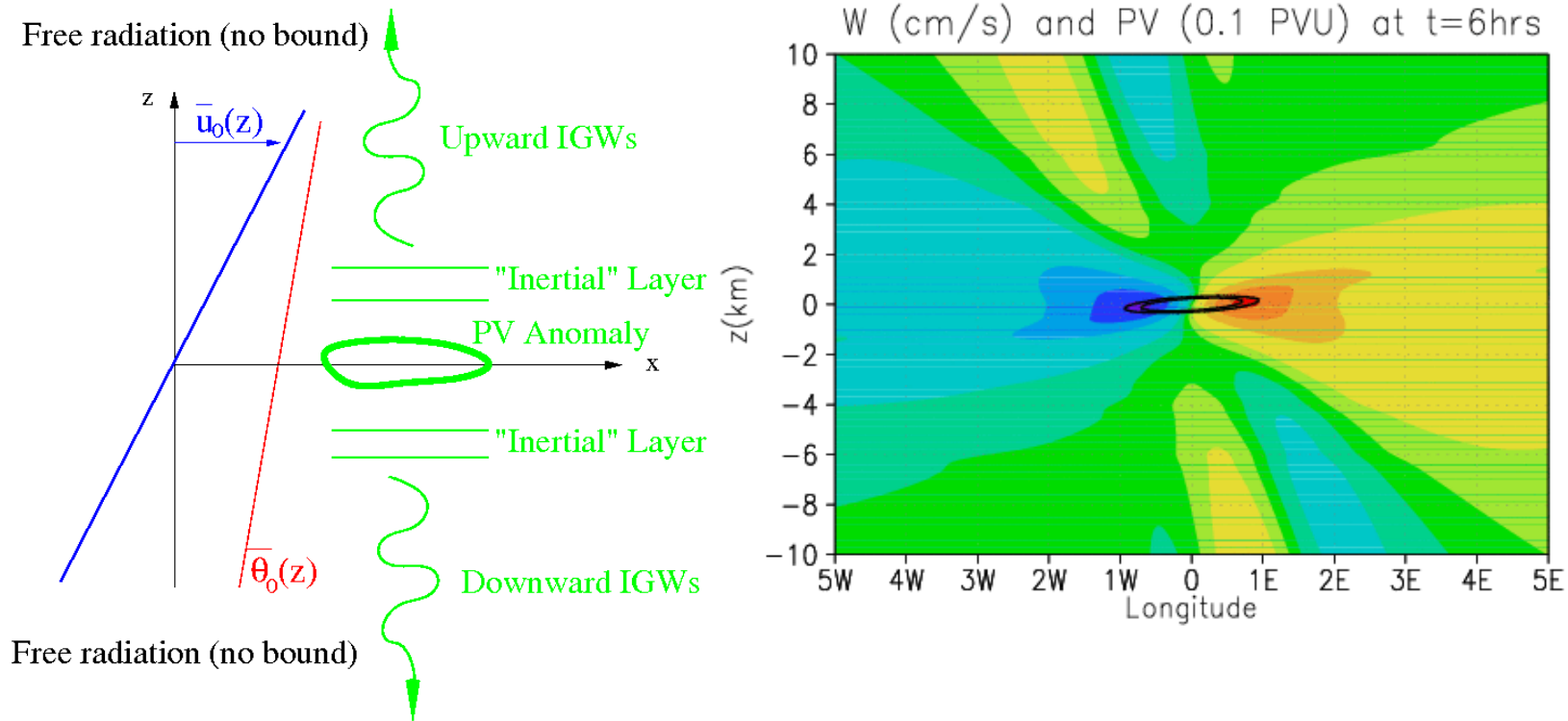
*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Well balanced means entirely described by the Potential vorticity distribution:

Spontaneous emission : GW emission from 3D (x,y,z) Potential Vorticity (PV) anomaly advected in a rotating ( $f = cte$ ), stratified ( $N = cte$ ) shear flow (vertical shear  $\Lambda = \bar{u}_{0z} = cte$ ).



Underlying justification : fronts are characterized by strong PV anomalies and wind shears

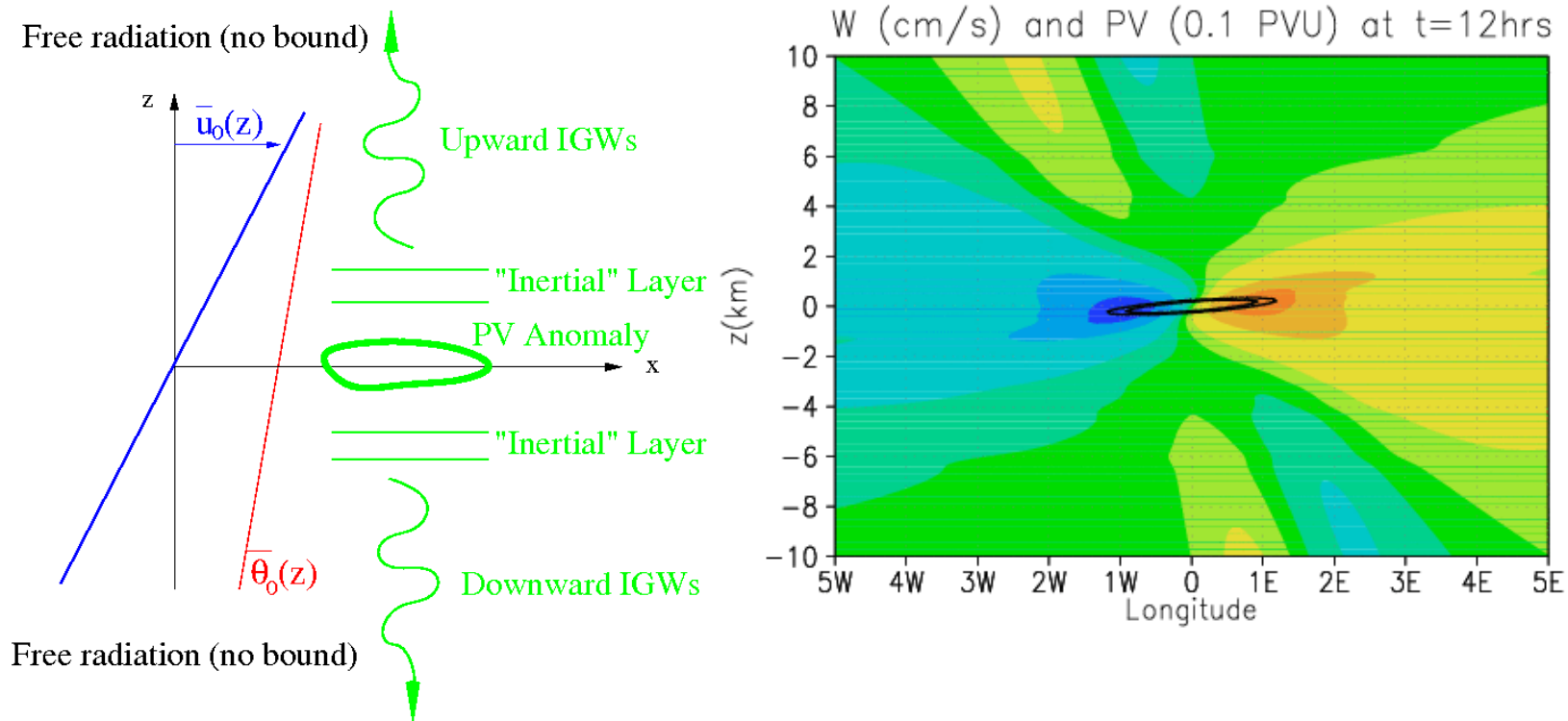
*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Well balanced means entirely described by the Potential vorticity distribution:

Spontaneous emission : GW emission from 3D (x,y,z) Potential Vorticity (PV) anomaly advected in a rotating ( $f = cte$ ), stratified ( $N = cte$ ) shear flow (vertical shear  $\Lambda = \bar{u}_{0z} = cte$ ).



Underlying justification : fronts are characterized by strong PV anomalies and wind shears

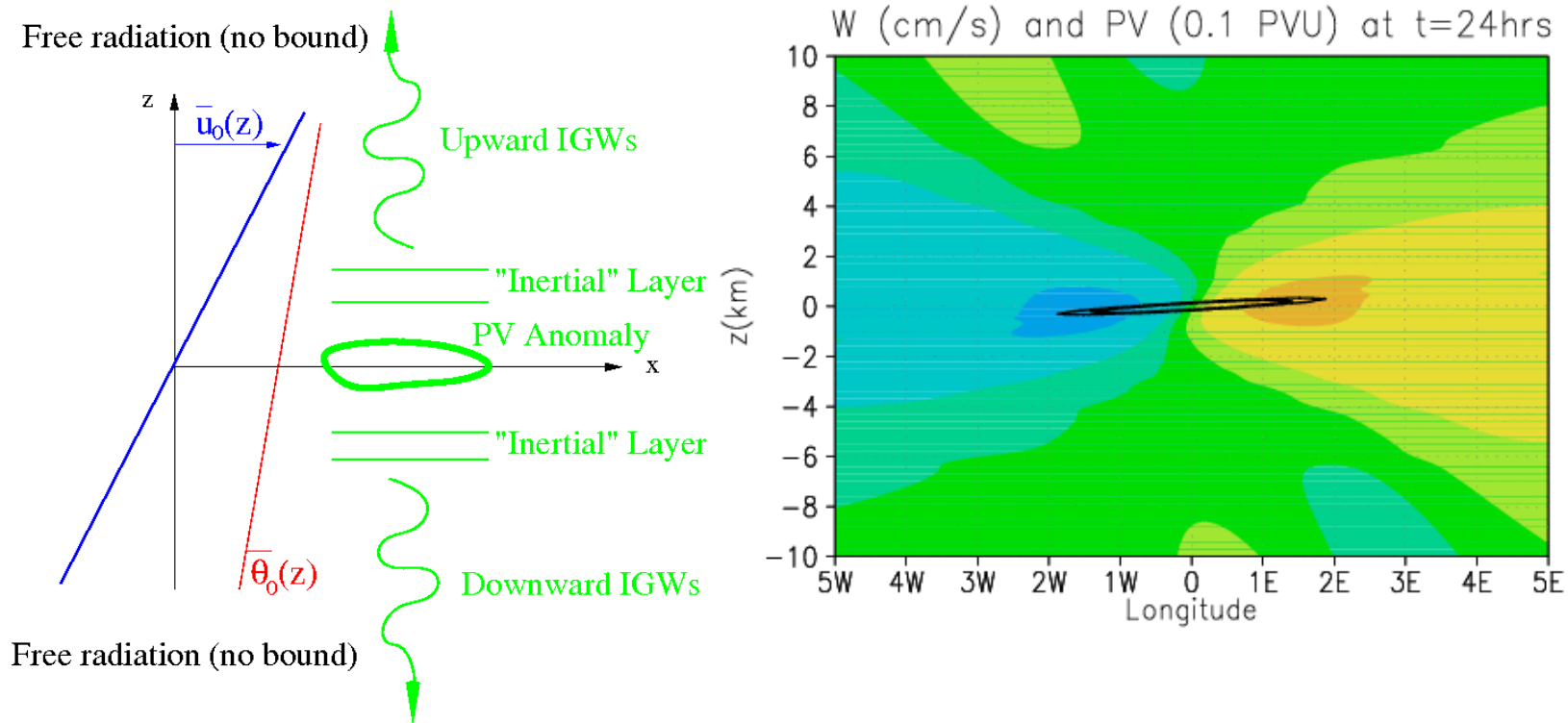
*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Well balanced means entirely described by the Potential vorticity distribution:

Spontaneous emission : GW emission from 3D (x,y,z) Potential Vorticity (PV) anomaly advected in a rotating ( $f = cte$ ), stratified ( $N = cte$ ) shear flow (vertical shear  $\Lambda = \bar{u}_{0z} = cte$ ).



Underlying justification : fronts are characterized by strong PV anomalies and wind shears

*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

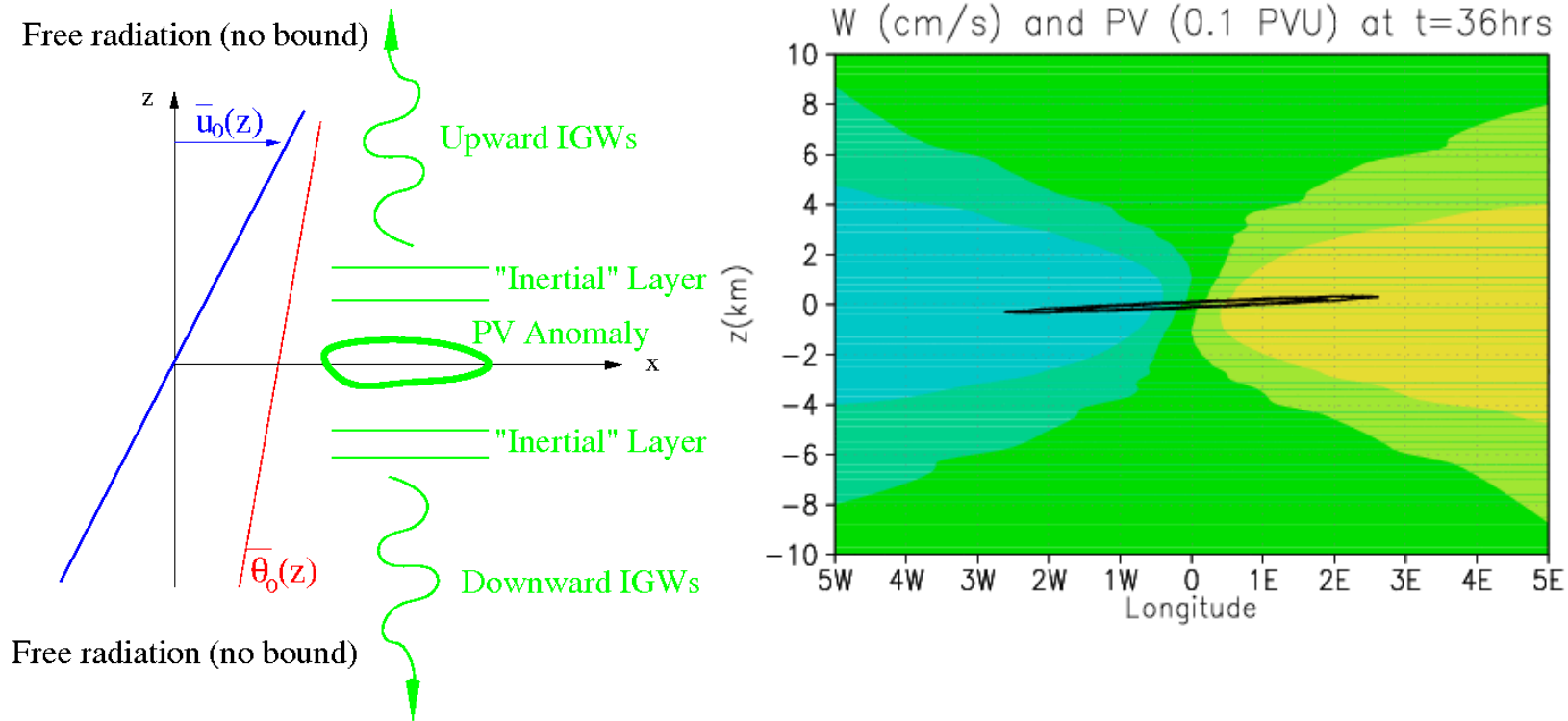


# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Well balanced means entirely described by the Potential vorticity distribution:

Spontaneous emission : GW emission from 3D (x,y,z) Potential Vorticity (PV) anomaly advected in a rotating ( $f = cte$ ), stratified ( $N = cte$ ) shear flow (vertical shear  $\Lambda = \bar{u}_{0z} = cte$ ).



Underlying justification : fronts are characterized by strong PV anomalies and wind shears

*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

The complete solution can be reconstructed from a single monochromatic solution:

$$w'(x, y, z, t) = \hat{w}_0(k, l, \omega) W(\xi) e^{i(kx + ly - \omega t)}$$

$$\xi = \frac{k\Lambda}{f}(z - z') = \frac{k\bar{u}_0(z) - \omega}{f}$$

$\xi=0$  Ordinary critical level  
(Intrinsic frequency=0)

$\xi=-1, +1$  Inertio critical levels  
(Intrinsic frequency =  $-f, +f$ )

$(\partial_t + \bar{u}_0 \partial_x)$   
Advection

Its vertical structure satisfies the PV conservation Eq:

$$\xi \left( \begin{array}{c} \text{Disturbance PV} \\ -W_{\xi\xi} + \left( \frac{W_{\xi}}{\xi^2} \right)_{\xi} + \left( \frac{2i\nu W}{\xi^2} \right)_{\xi} - \frac{J(1 + \nu^2)}{\xi^2} W \end{array} \right) = 0$$

$$\text{QG PV: } f \partial_z \theta' + \bar{\theta}_{0z} (\partial_x v' - \partial_y u')$$

Richardson number  $J = N^2 / \Lambda^2$  ; Hor. Wavenumber ratio  $\nu = l/k$

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

The canonical solution  $W(\xi)$  corresponds to a  $\delta(\xi)$ -PV distribution:

$$-W_{\xi\xi} + \left(\frac{W_\xi}{\xi^2}\right)_\xi + \left(\frac{2i\nu W}{\xi^2}\right)_\xi - \frac{J(1+\nu^2)}{\xi^2} W = \delta(\xi)$$

$J=5, |\nu| \ll 1$

$\xi \gg 1$ :  $E \xi^{1/2+i\mu}$  (upward GW)

$\xi > 1$ :  $E (1+\xi)^{-i\nu} \xi^{1/2+i\nu+i\mu} F(1-\xi^{-2})$

In  $\xi=1$  the CL continuation links E with A and B

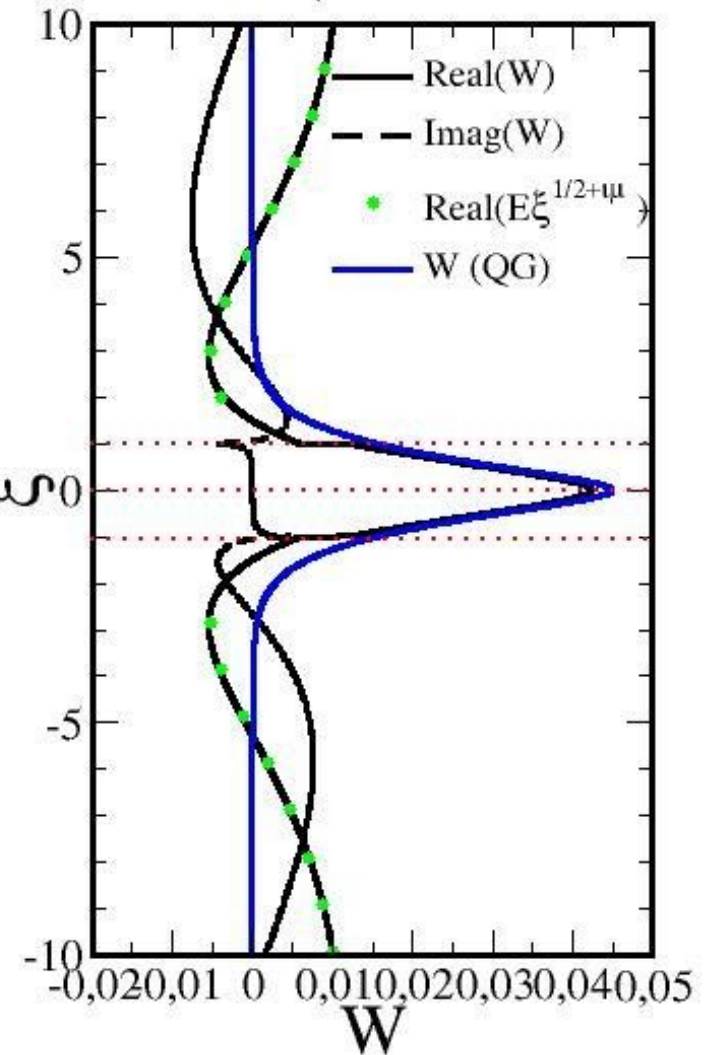
$0 < \xi < 1$ :  $(1+\xi)^{-i\nu} (A F'(\xi^2) + B \xi^3 F''(\xi^2))$

B and A such that  $W_\xi/\xi^2(0^+) - W_\xi/\xi^2(0^-) = 1$

$-1 < \xi < 0$ :  $(1-\xi)^{+i\nu} (A^* F'^*(\xi^2) - B^* \xi^3 F''^*(\xi^2))$

$\xi \ll -1$ :  $E^* |\xi|^{1/2-i\mu}$  (downward GW)

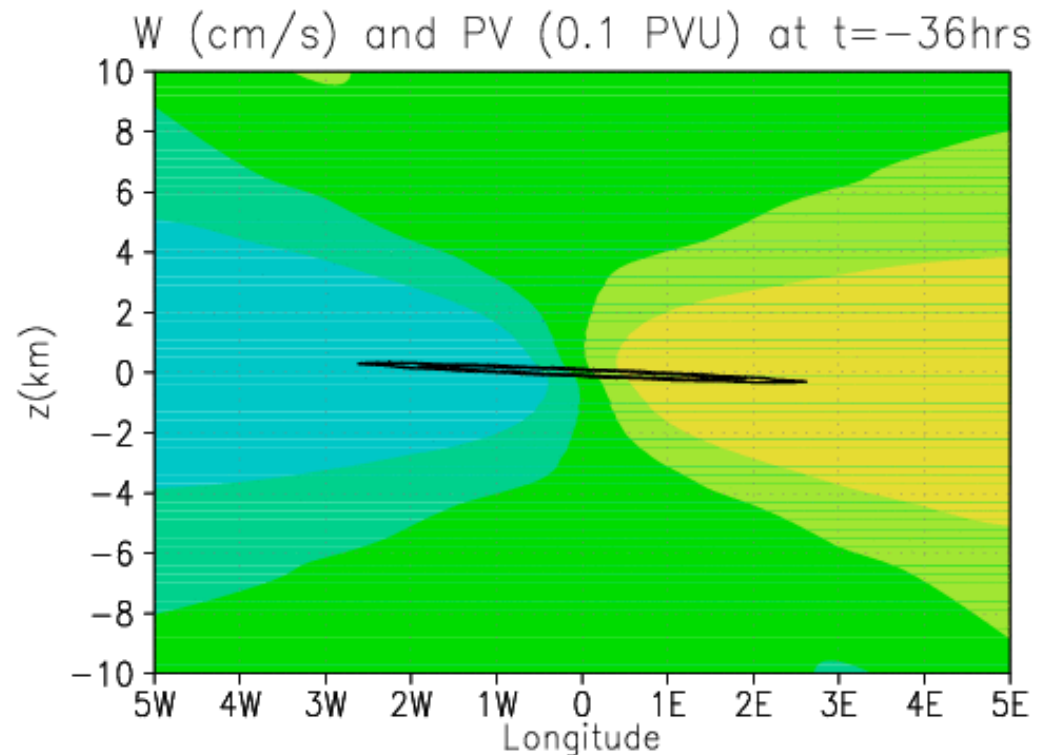
$F, F',$  and  $F''$  Hypergeometric functions



# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

General setup: A 3D (x,y,z) PV anomaly advected in a rotating ( $f=cte$ ), stratified (BV freq  $N=cte$ ) shear flow (vertical shear  $\Lambda=cte$ ).

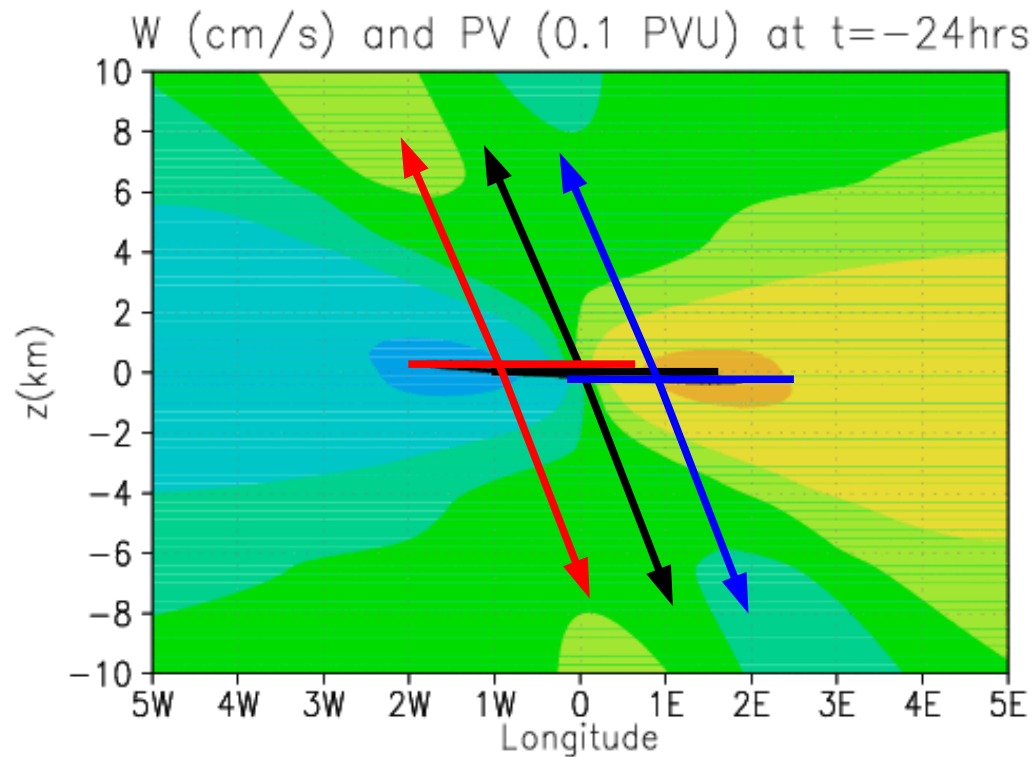


$$wN^2 \sim f\Lambda v$$

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

General setup: A 3D (x,y,z) PV anomaly advected in a rotating ( $f=cte$ ), stratified (BV freq  $N=cte$ ) shear flow (vertical shear  $\Lambda=cte$ ).



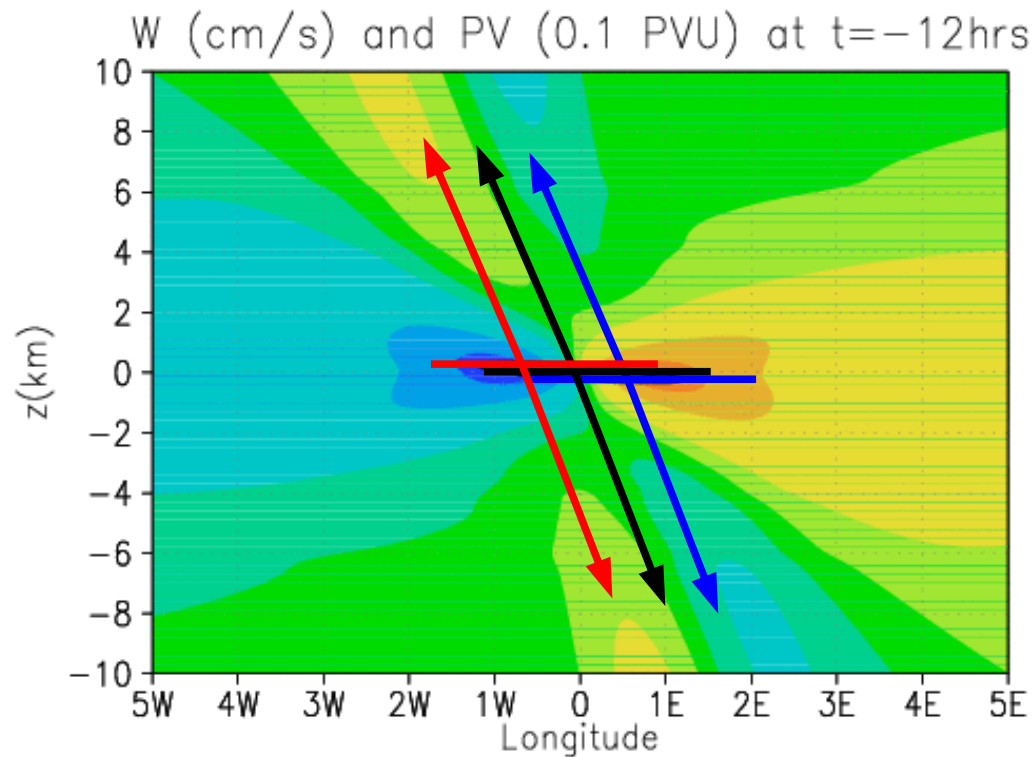
*Lott, Plougonven and Vanneste, JAS 2010, 2012.*



# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

General setup: A 3D (x,y,z) PV anomaly advected in a rotating ( $f=cte$ ), stratified (BV freq  $N=cte$ ) shear flow (vertical shear  $\Lambda=cte$ ).

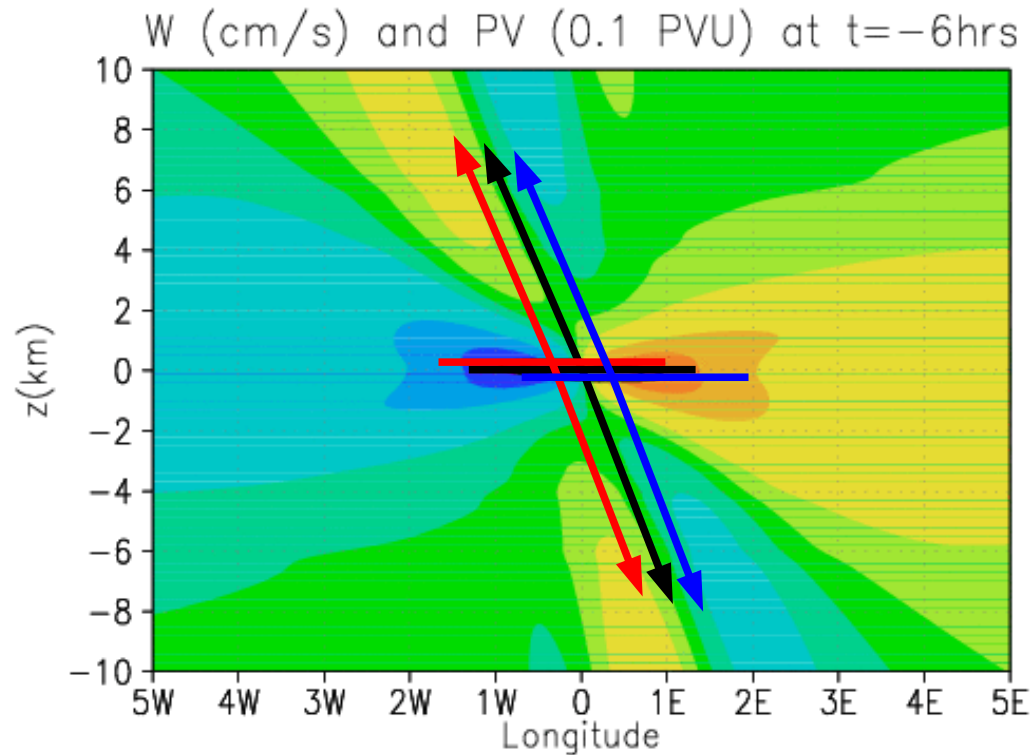


*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

General setup: A 3D (x,y,z) PV anomaly advected in a rotating ( $f=cte$ ), stratified (BV freq  $N=cte$ ) shear flow (vertical shear  $\Lambda=cte$ ).

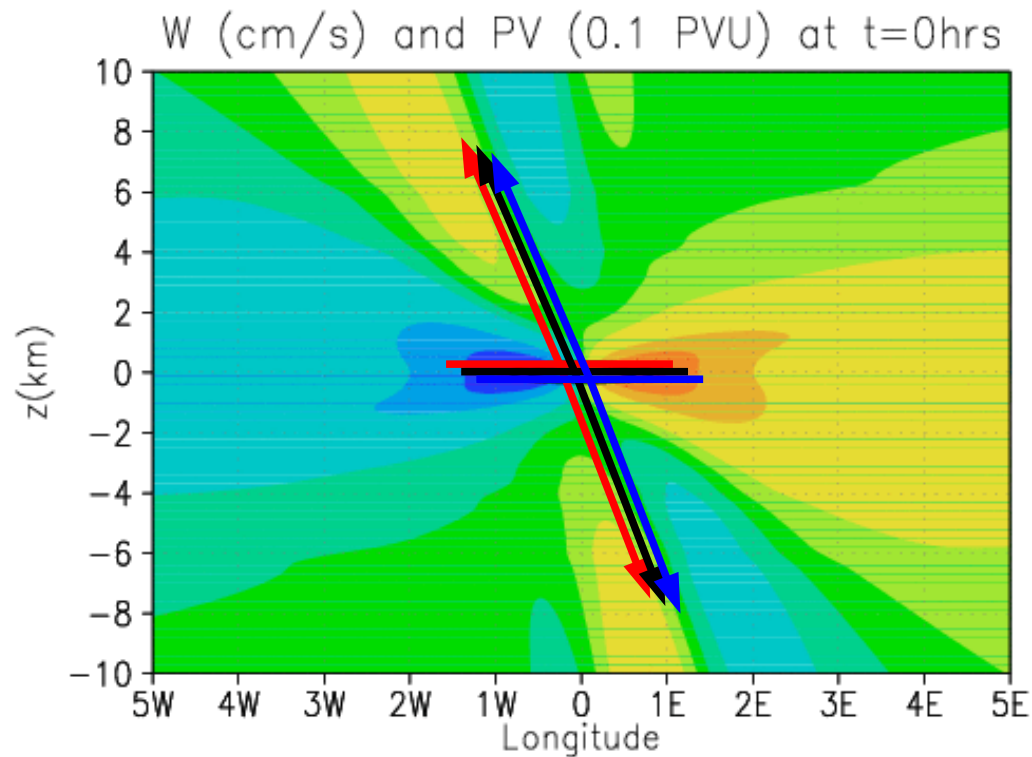


*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

General setup: A 3D (x,y,z) PV anomaly advected in a rotating ( $f=\text{cte}$ ), stratified (BV freq  $N=\text{cte}$ ) shear flow (vertical shear  $\Lambda=\text{cte}$ ).

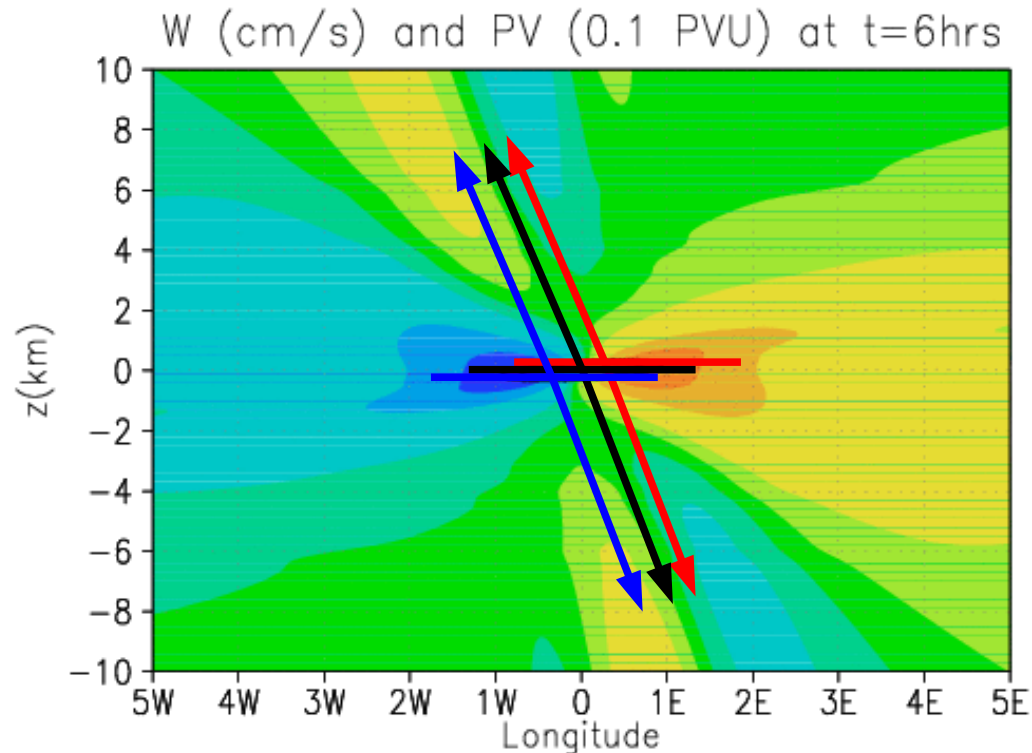


*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

General setup: A 3D (x,y,z) PV anomaly advected in a rotating ( $f=\text{cte}$ ), stratified (BV freq  $N=\text{cte}$ ) shear flow (vertical shear  $\Lambda=\text{cte}$ ).

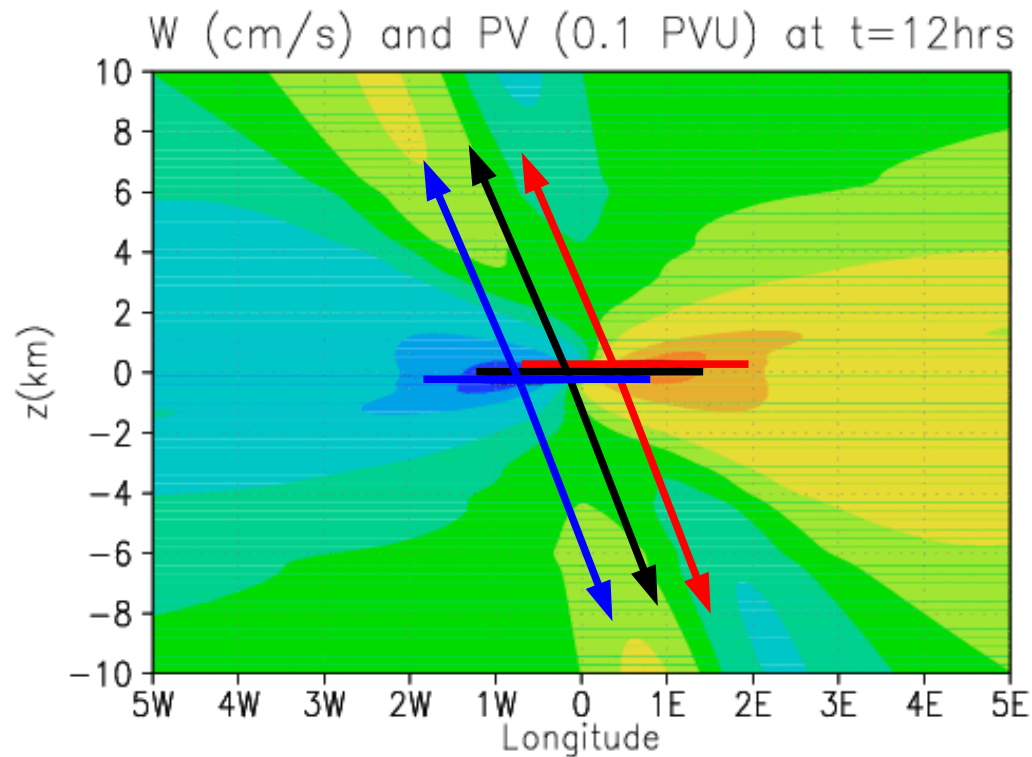


*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

General setup: A 3D (x,y,z) PV anomaly advected in a rotating ( $f=cte$ ), stratified (BV freq  $N=cte$ ) shear flow (vertical shear  $\Lambda=cte$ ).



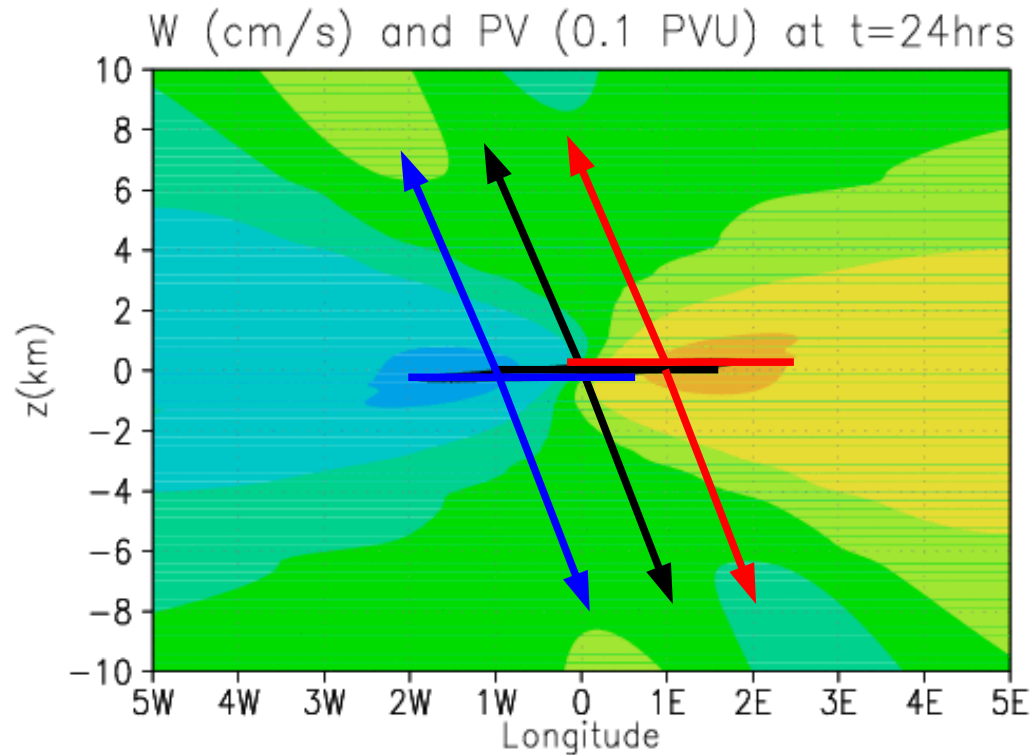
*Lott, Plougonven and Vanneste, JAS 2010, 2012.*



# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

General setup: A 3D (x,y,z) PV anomaly advected in a rotating ( $f=\text{cte}$ ), stratified (BV freq  $N=\text{cte}$ ) shear flow (vertical shear  $\Lambda=\text{cte}$ ).

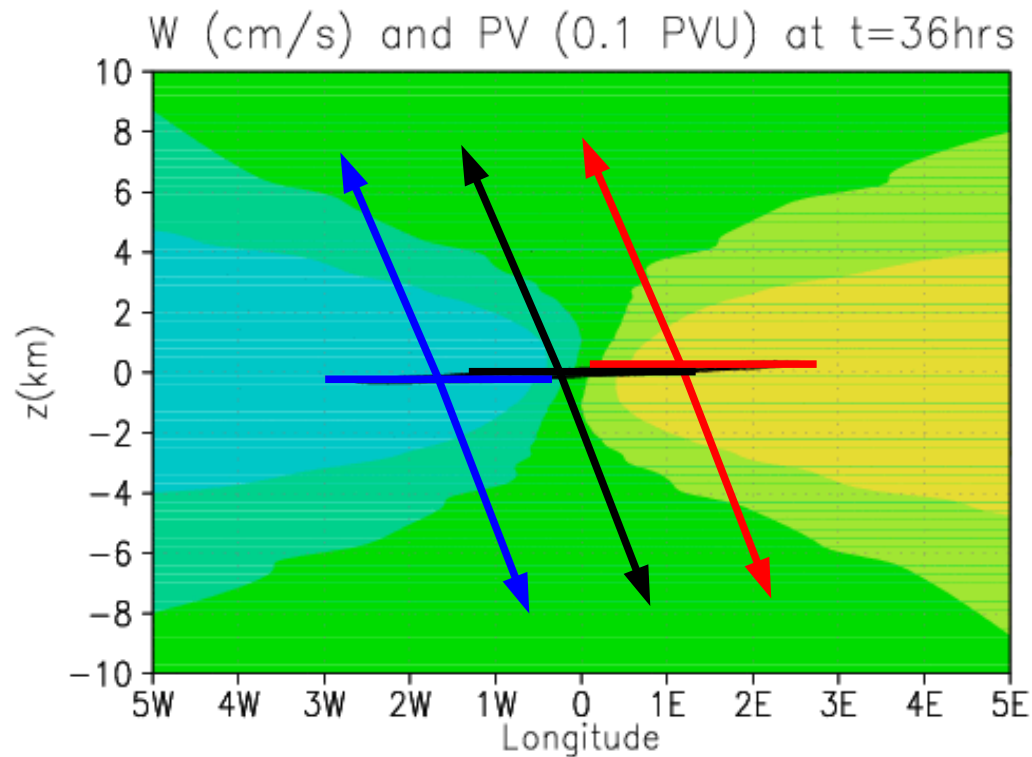


*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

General setup: A 3D (x,y,z) PV anomaly advected in a rotating ( $f=cte$ ), stratified (BV freq  $N=cte$ ) shear flow (vertical shear  $\Lambda=cte$ ).



*Lott, Plougonven and Vanneste, JAS 2010, 2012.*

## Parameterization of GWs in large scale models

### 4) Application to gravity waves generated by fronts

The wave stress is predictable in closed analytical form:

$$F \approx \frac{\rho g^2}{f \theta^2 N^3} (\rho q' \sigma_z)^2 \frac{e^{-\pi \frac{N}{\Lambda}}}{4}$$

↑ PV anomaly
↑ Characteristic depth of the PV anomaly

Valid for various PV distributions, and over long time scale (compared to the ½ hour interval at which subgrid-scale parameterisation routines are updated)

We next take for the PV  $q$  the GCM gridscale PV anomalies (as a measure of the subgrid scales one, again a “white” spectrum *hypothesis*)

Including the frontal waves, see next presentation, now it is the subgrid scale vorticity which is considered as a “white” stochastic series:

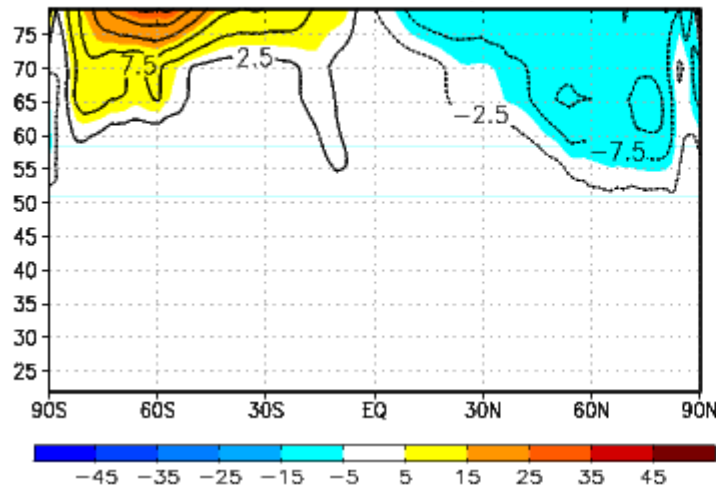
$$q' = \sum_{n=1}^{\infty} C_n q_n' \quad \text{where} \quad q_n' = \Re \left[ \hat{q}_n e^{i(\vec{k}_n \cdot \vec{x} - \omega_n t)} \right] \quad \text{taking} \quad |\hat{q}_n| = |q_r|$$

# Parameterization of GWs in large scale models

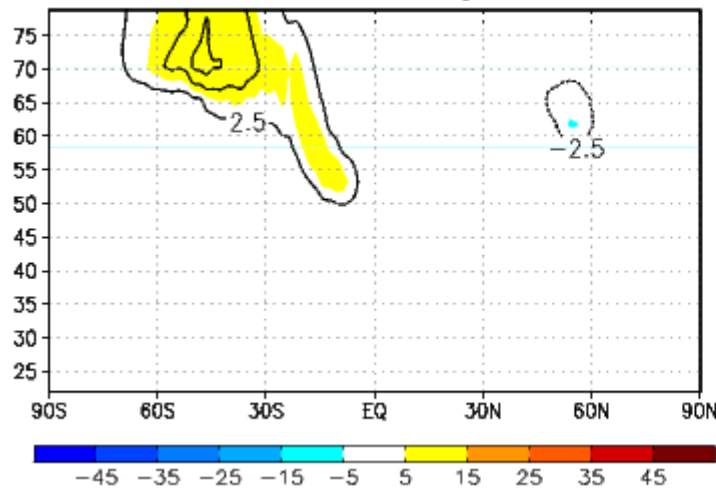
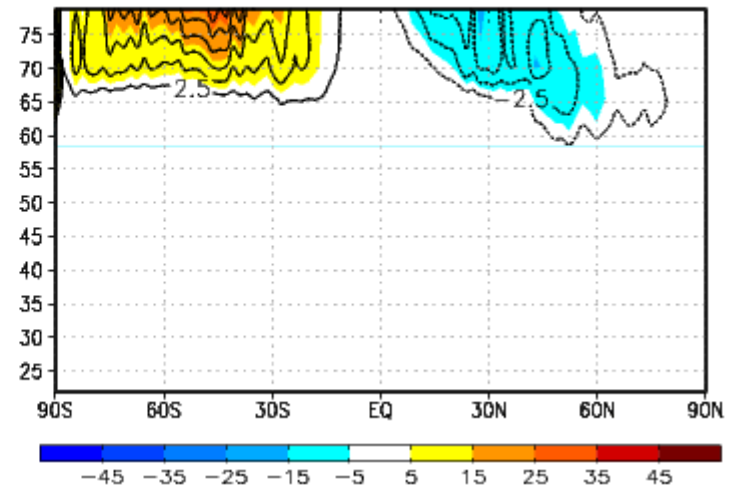
## 4) Application to gravity waves generated by fronts

The theory predicts about the right amount of drag compared to a highly tuned globally spectral scheme (January, all in m/s/day)

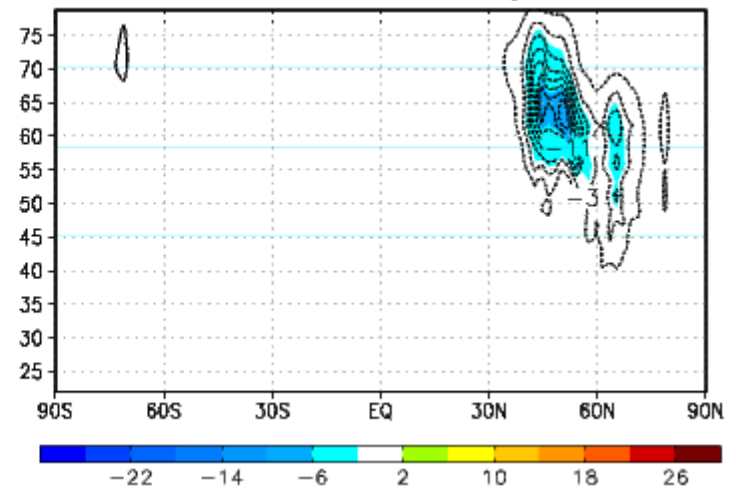
Globally spectral scheme



From fronts



Convective GWs

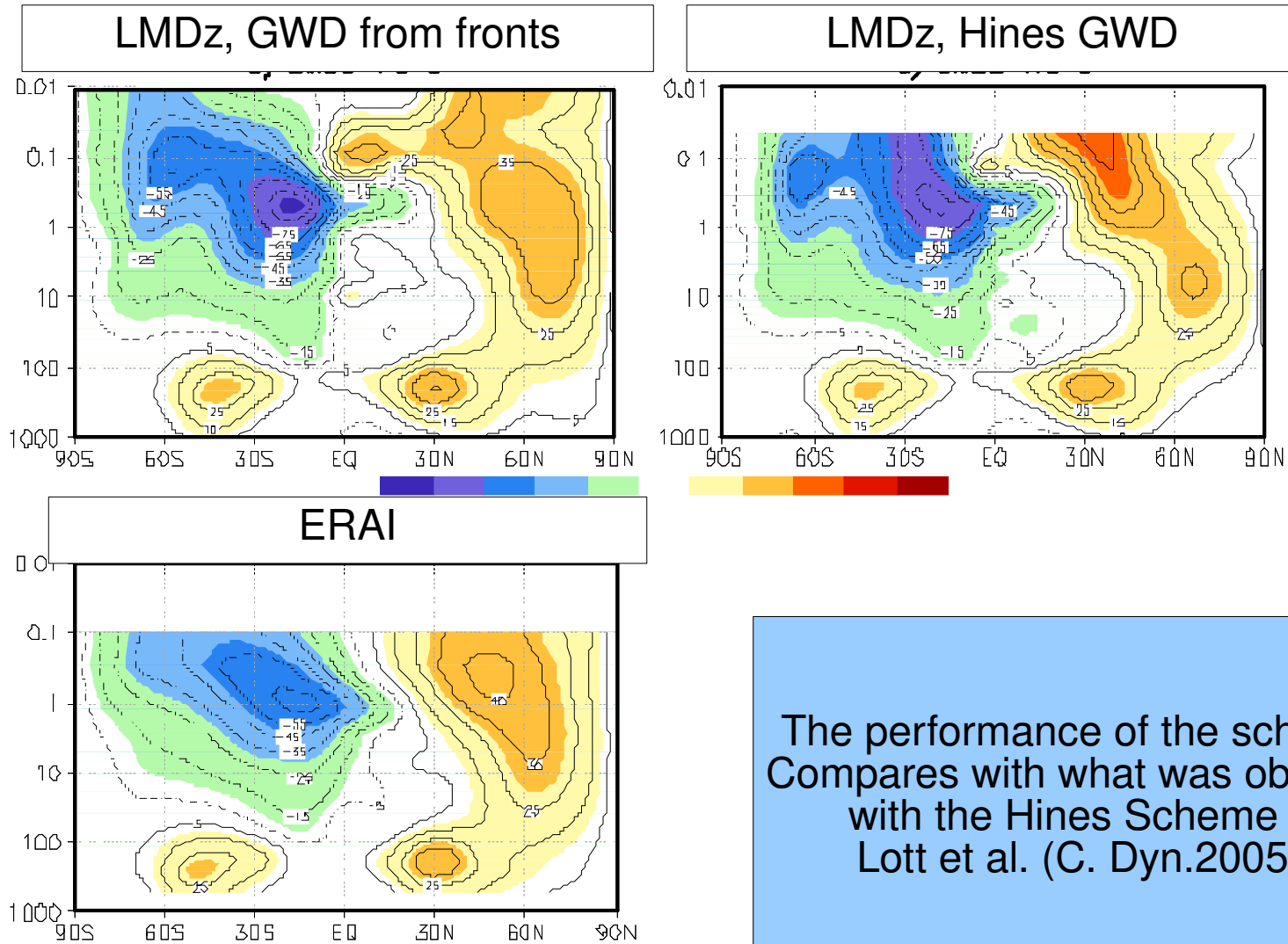


Mountains GWs

# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Zonal wind U, January climatology



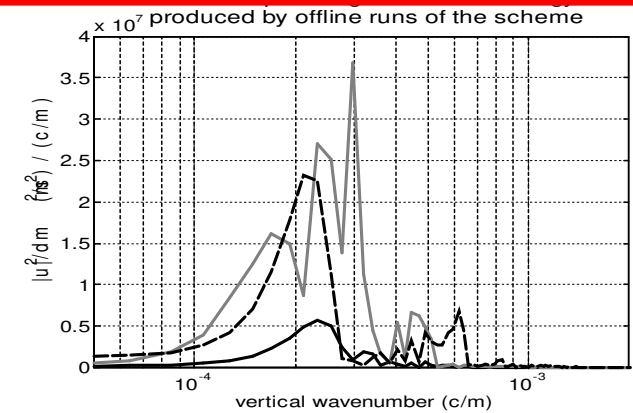
The performance of the scheme  
Compares with what was obtained  
with the Hines Scheme in  
Lott et al. (C. Dyn.2005,)

# Parameterization of GWs in large scale models

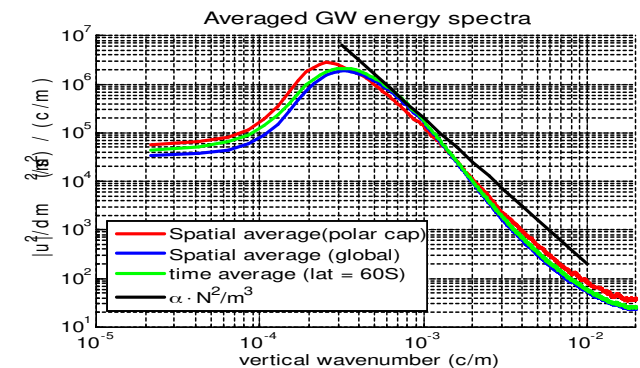
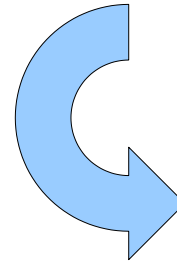
## 4) Application to gravity waves generated by fronts

### Vertical spectra of GWs energy

The observed “universal spectra” can be obtained with a “multiwave scheme” as a superposition of individual periodograms of GW packets.



Average of  
periodograms

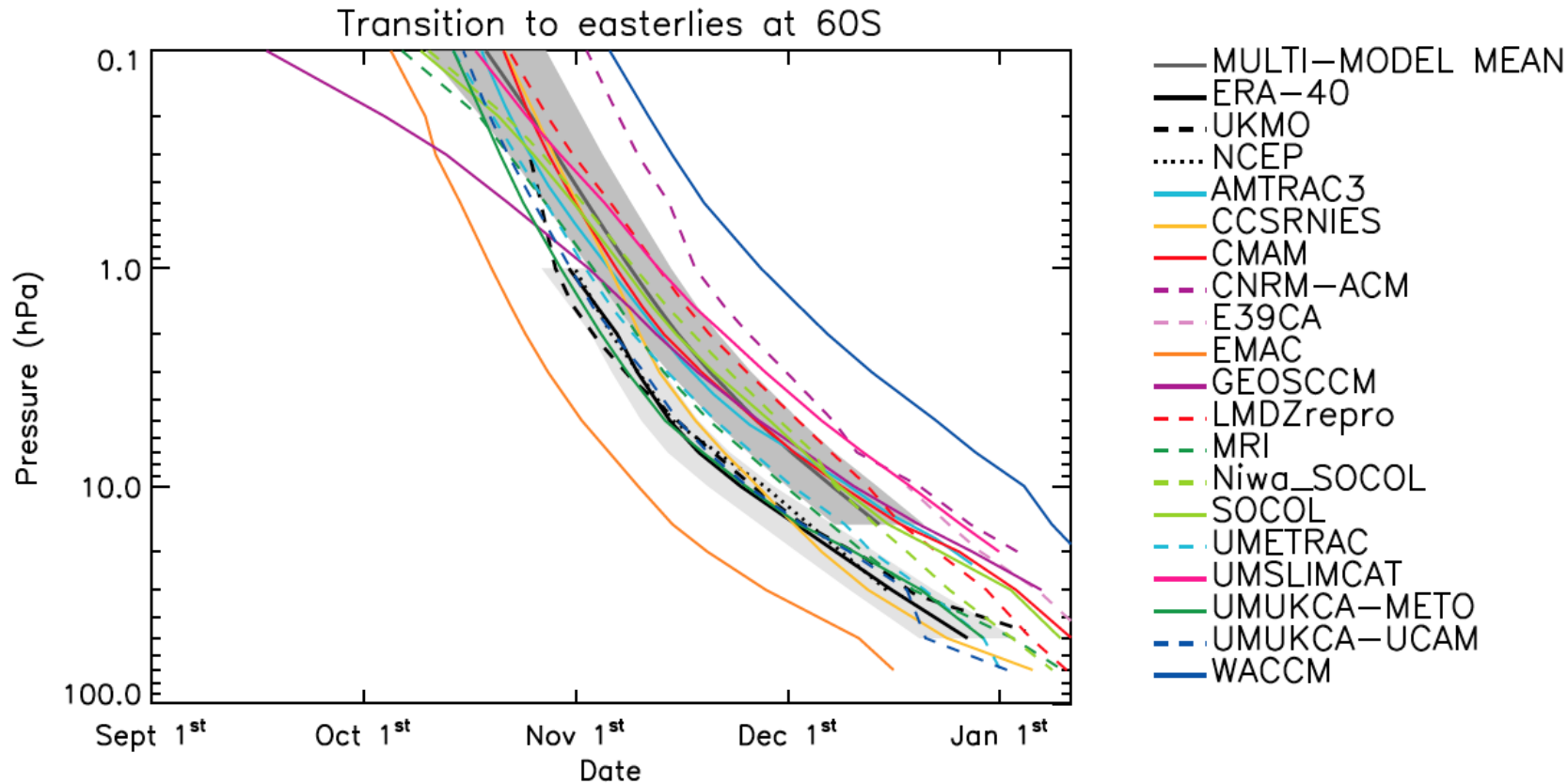




# Parameterization of GWs in large scale models

## 4) Application to gravity waves generated by fronts

Butchart et al. 2011, *JGR*, *date when  $u(60S)$  fall below 10m/s*



**Insufficient parameterized GW drag at 60°S as cause of late final warming bias**

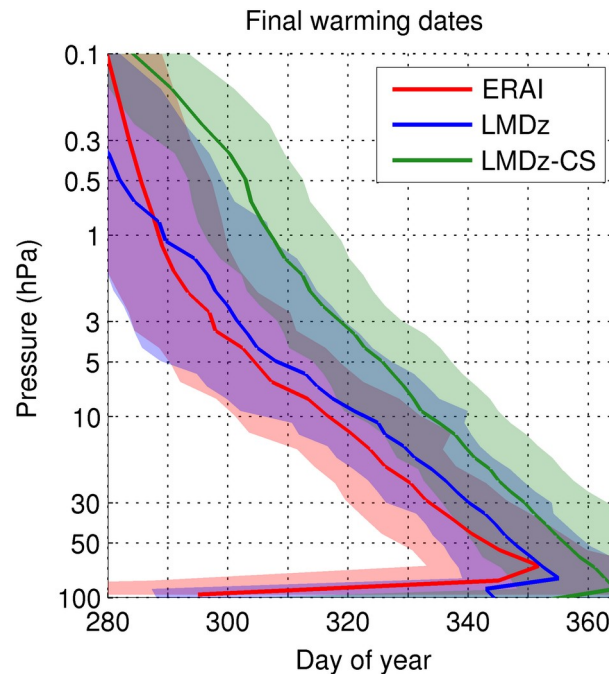
(McLandress et al., 2012 *JAS*)

Due to lateral propagation of orographic waves? (Sato et al. 2009)

## Parameterization of GWs in large scale models

### 4) Application to gravity waves generated by fronts

Test with constant sources (CS) against source related Gws.  
Source related GWs predict an earlier breakdown  
(Effect due to intermittency again?)



In the SH, the final warming dates times the winter vortex breakdown:  
date when  $u(60S)$  fall below 10m/s

# Parameterization of GWs in large scale models

## 5) Validation against balloon observations

### Mid latitudes and Concordiasi

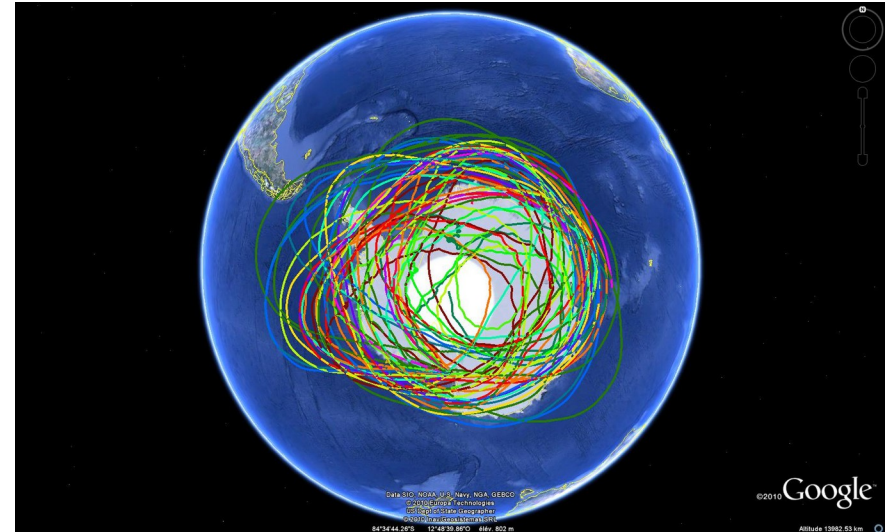
#### GWs from the scheme:

Offline runs using ERAI and GPCP data corresponding to the Concordiasi period.

Important: Satellite (partial) observations in the tropics support what is shown next.



[www.lmd.polytechnique.fr/VORCORE/Djournal2/Journal.htm](http://www.lmd.polytechnique.fr/VORCORE/Djournal2/Journal.htm)



### CONCORDIASI (2010)

*Rabier et al. 2010 BAMS*

19 super-pressure balloons launched from McMurdo, Antarctica, during Sep and Oct 2010.

The balloons were at ~ 20 km height.

Dataset of GW momentum fluxes (*as by Hertzog et al. 2008*)

[www.lmd.polytechnique.fr/VORCORE/Djournal2/Journal.htm](http://www.lmd.polytechnique.fr/VORCORE/Djournal2/Journal.htm)

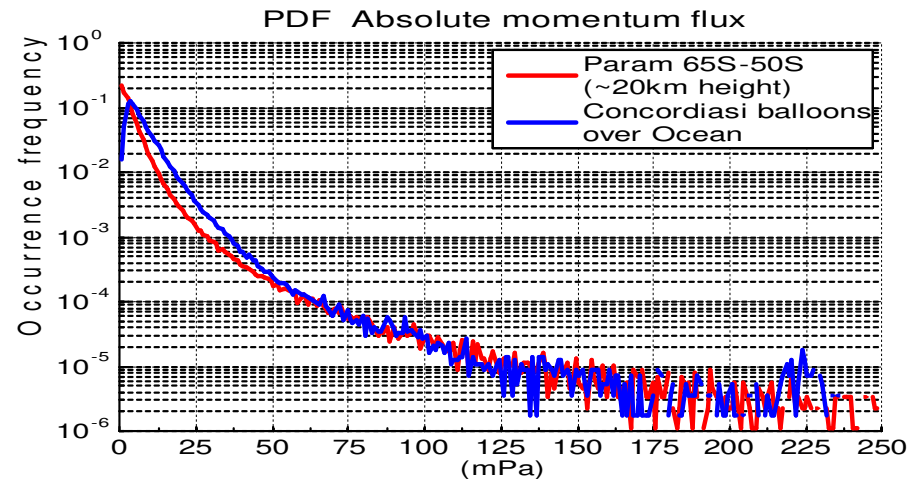
# Parameterization of GWs in large scale models

## 5) Validation against balloon observations

### Mid latitudes and Concordiasi Intermittency of GW momentum flux

The stochastic scheme parameters can be tuned to produce fluxes as intermittent as in balloon observations.

An effect in good part due to the inclusion of the sources (convective and frontal)



Intermittency is important because it produces GW breaking at lower altitudes (*Lott&Guez 2013*,  
*de la Cámara et al. 2015*)



Parameterization of GWs in large scale models  
5) Validation against balloon observations

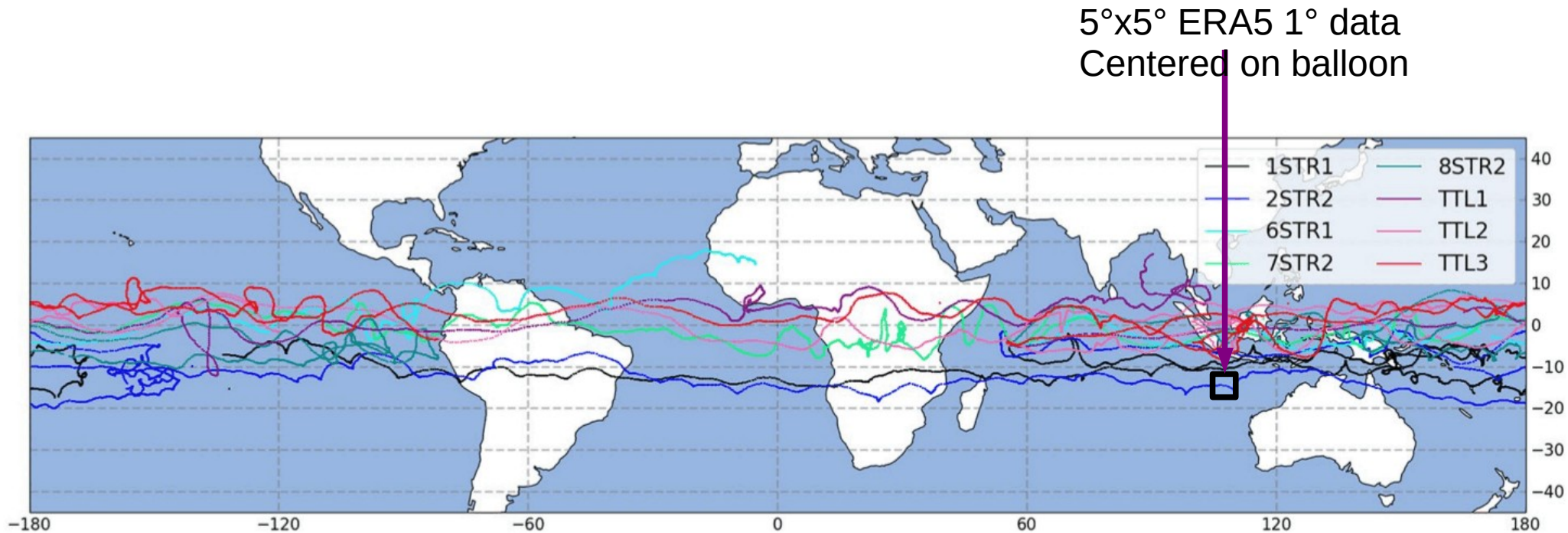
**Convective gravity waves and the tropics : Strateole 2**

Strateole 2, period 1 (Nov.2019-Feb. 2020, Corcos et al. 2021)



Parameterization of GWs in large scale models  
5) Validation against balloon observations

**Convective gravity waves and the tropics : Strateole 2**



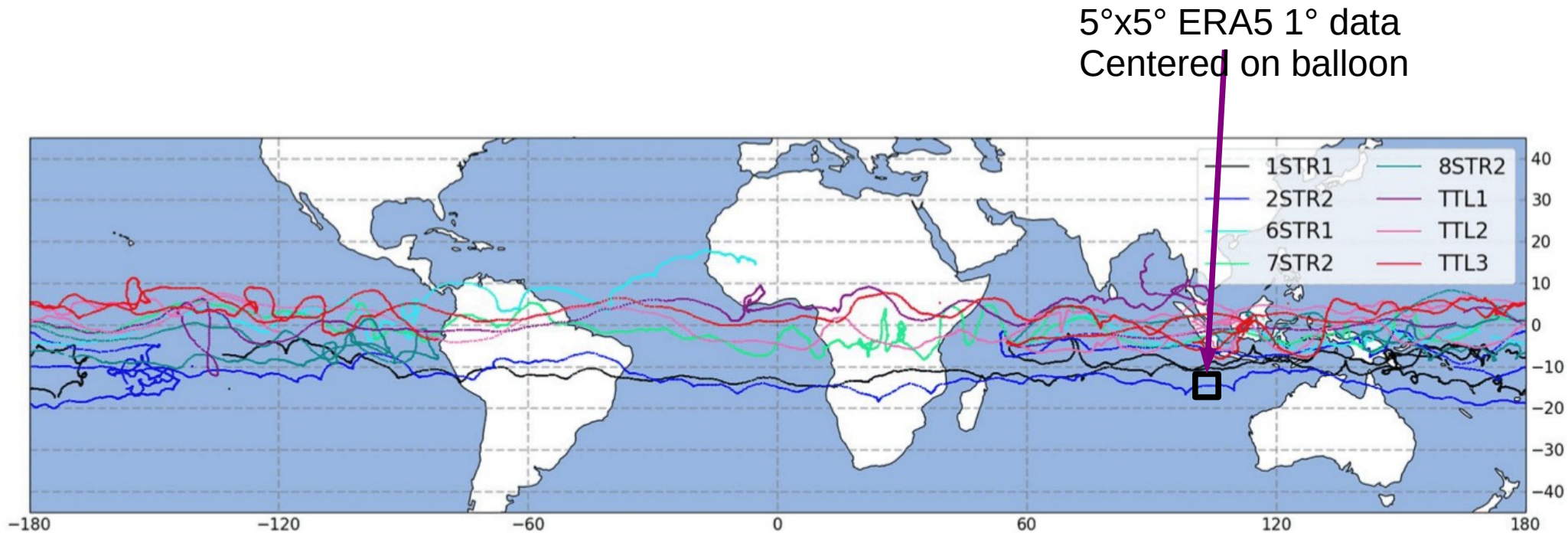
**Strateole 2 phase 1, Nov 2019-Feb . 2020**  
**8 Balloon 2- to 3 months flights at about z=20km**

Adapted from Corcos et al. JGR2021

# Parameterization of GWs in large scale models

## 5) Validation against balloon observations

### Convective gravity waves and the tropics : Strateole 2



**Strateole 2 phase 1, Nov 2019-Feb . 2020**  
**8 Balloon 2- to 3 months flights at about z=20km**

Adapted from Corcos et al. JGR2021

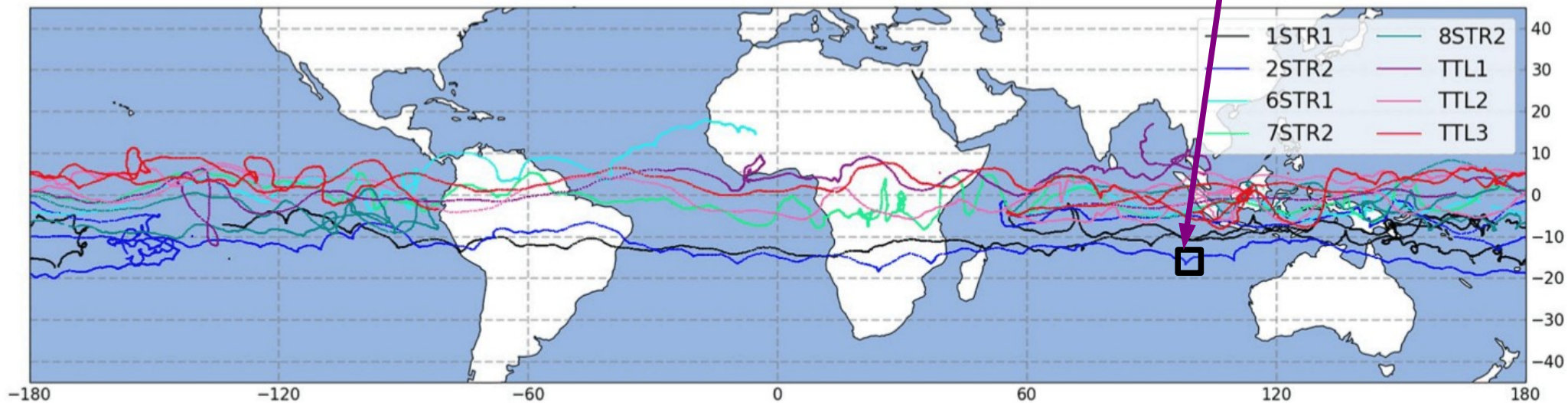


# Parameterization of GWs in large scale models

## 5) Validation against balloon observations

### Convective gravity waves and the tropics : Strateole 2

5°x5° ERA5 1° data  
Centered on balloon



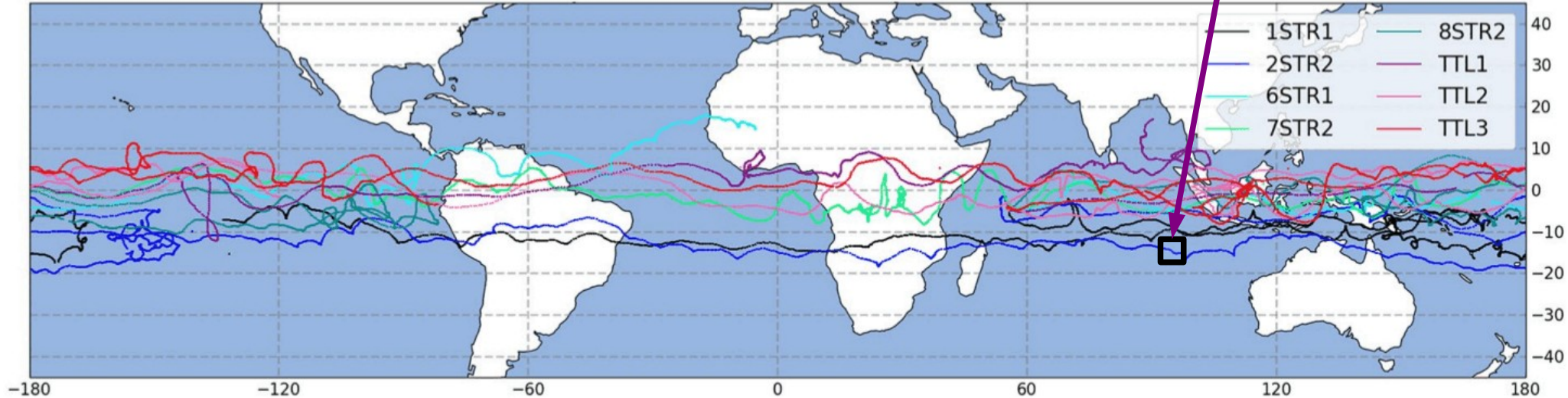
**Strateole 2 phase 1, Nov 2019-Feb . 2020**  
**8 Balloon 2- to 3 months flights at about z=20km**

Adapted from Corcos et al. JGR2021

Parameterization of GWs in large scale models  
5) Validation against balloon observations

**Convective gravity waves and the tropics : Strateole 2**

5°x5° ERA5 1° data  
Centered on balloon



**Strateole 2 phase 1, Nov 2019-Feb . 2020**

**8 Balloon 2- to 3 months flights at about z=20km**

Adapted from Corcos et al. JGR2021

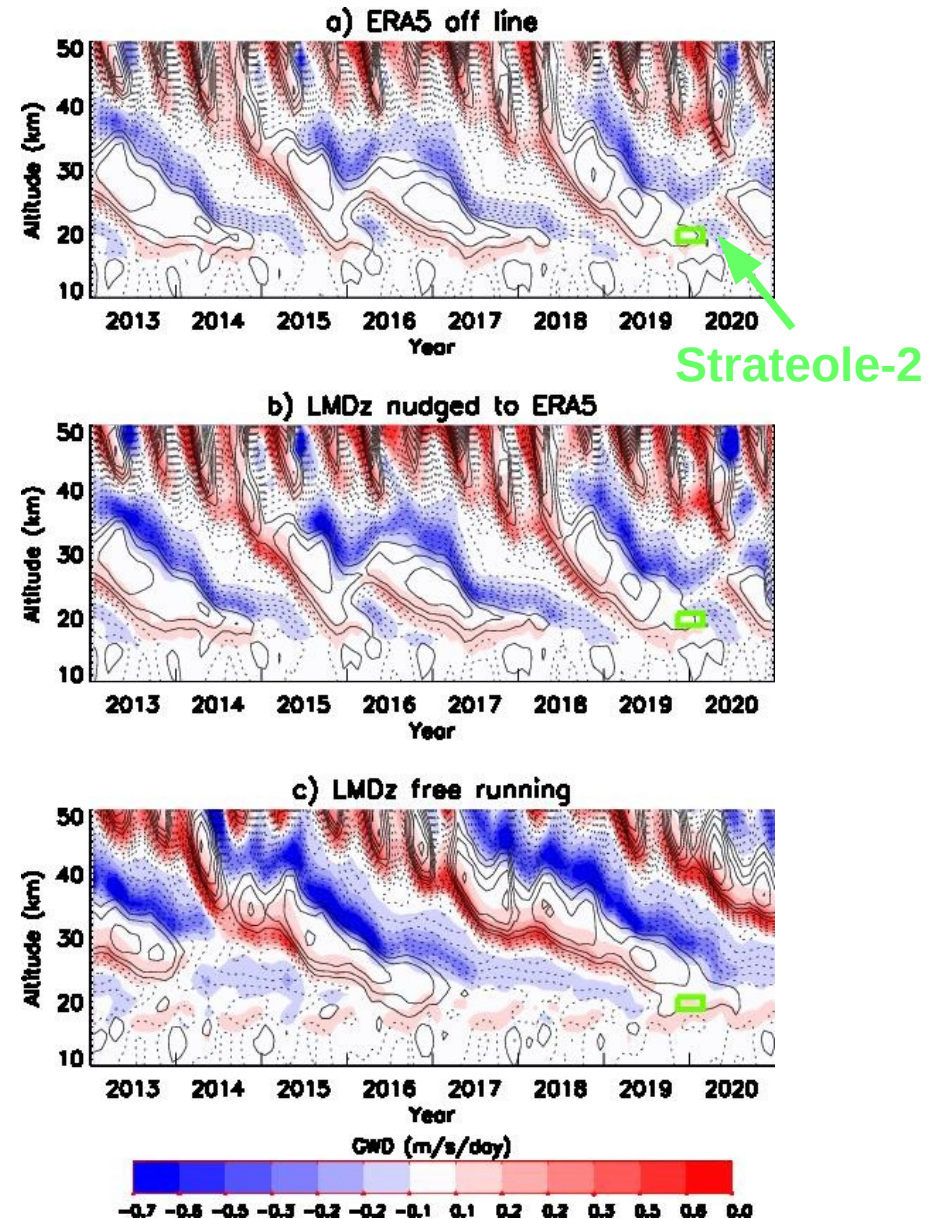
# Parameterization of GWs in large scale models

## 5) Validation against balloon observations

### Convective gravity waves and the tropics : Strateole 2

## Online-offline and nudge results with LMDz, large scale Fields from ERA5

GWD tendencies from Lott et al. (2013),  
adapted to IPSLCM6 Hourdin et al. (2020)



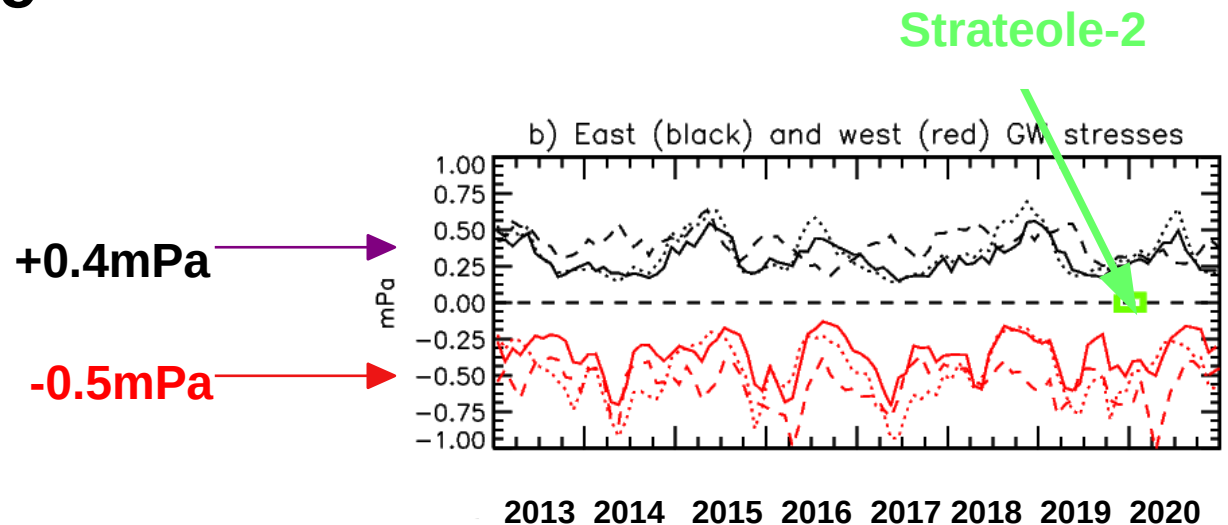


Parameterization of GWs in large scale models  
5) Validation against balloon observations

Convective gravity waves and the tropics : **Strateole 2**

Online-offline  
and nudge results  
with LMDz, large scale  
Fields from ERA5

East and **west** stress at  $z=20\text{km}$



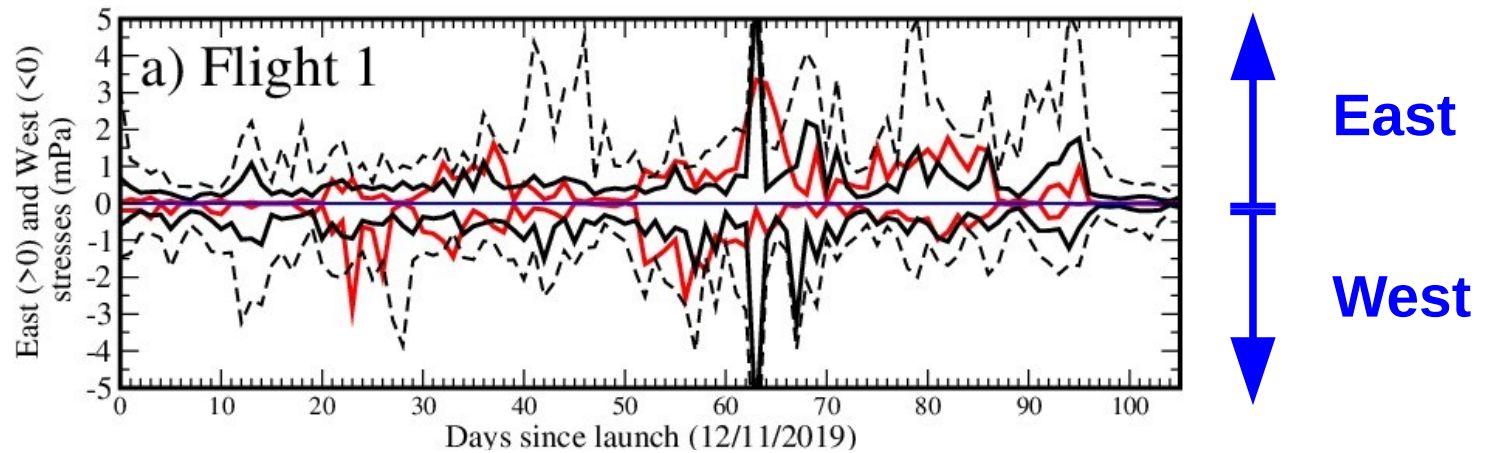
Zonally Averaged fluxes at about  $z=20\text{ km}$   
have values around 0.4-0.5mPa

# Parameterization of GWs in large scale models

## 5) Validation against balloon observations

### Convective gravity waves and the tropics : Strateole 2

Good correspondance between observation and **prediction** (15mn-1hr waves)

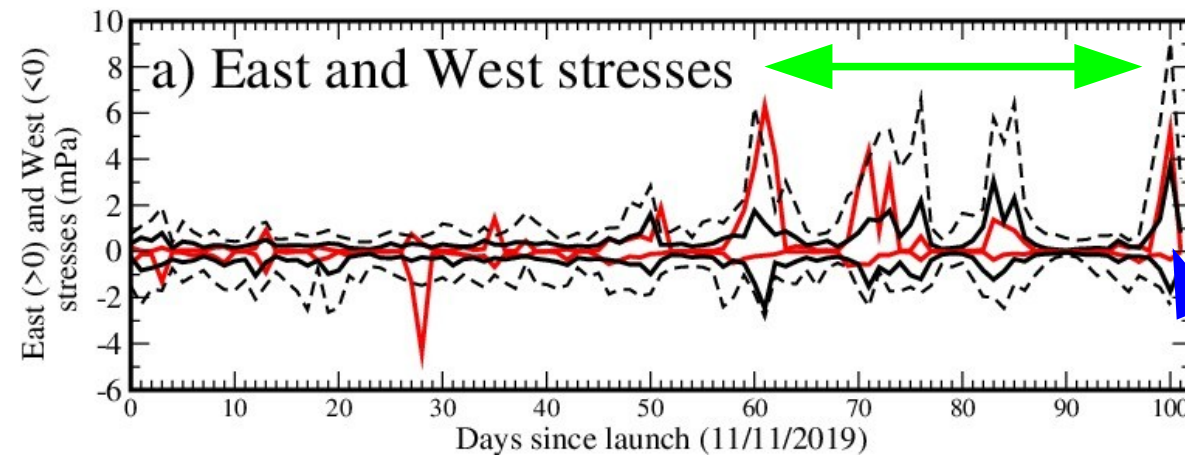


# Parameterization of GWs in large scale models

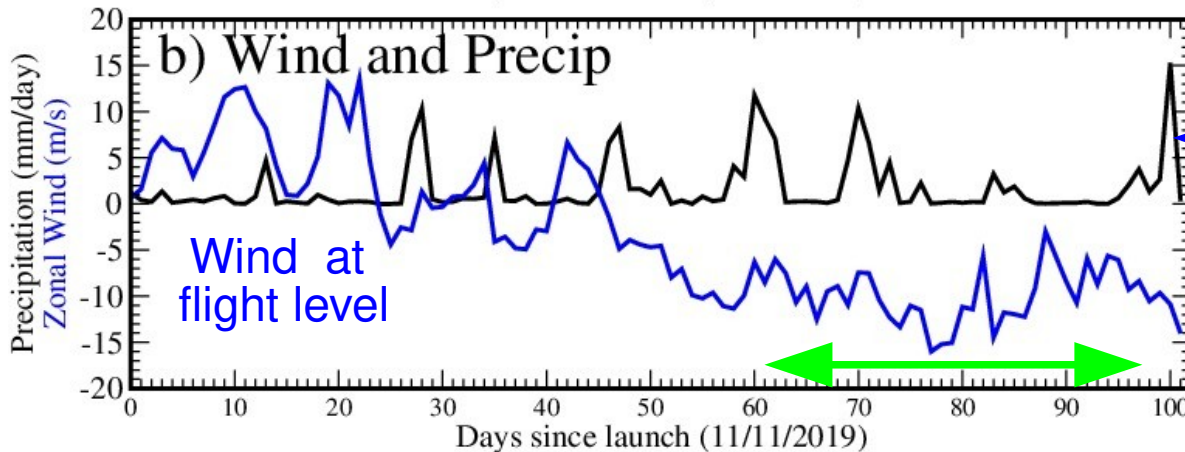
## 5) Validation against balloon observations

### Convective gravity waves and the tropics : Strateole 2

Evidence of dynamical filtering and relation with precipitation, case of Flight 2



More Eastward flux when Wind is westward



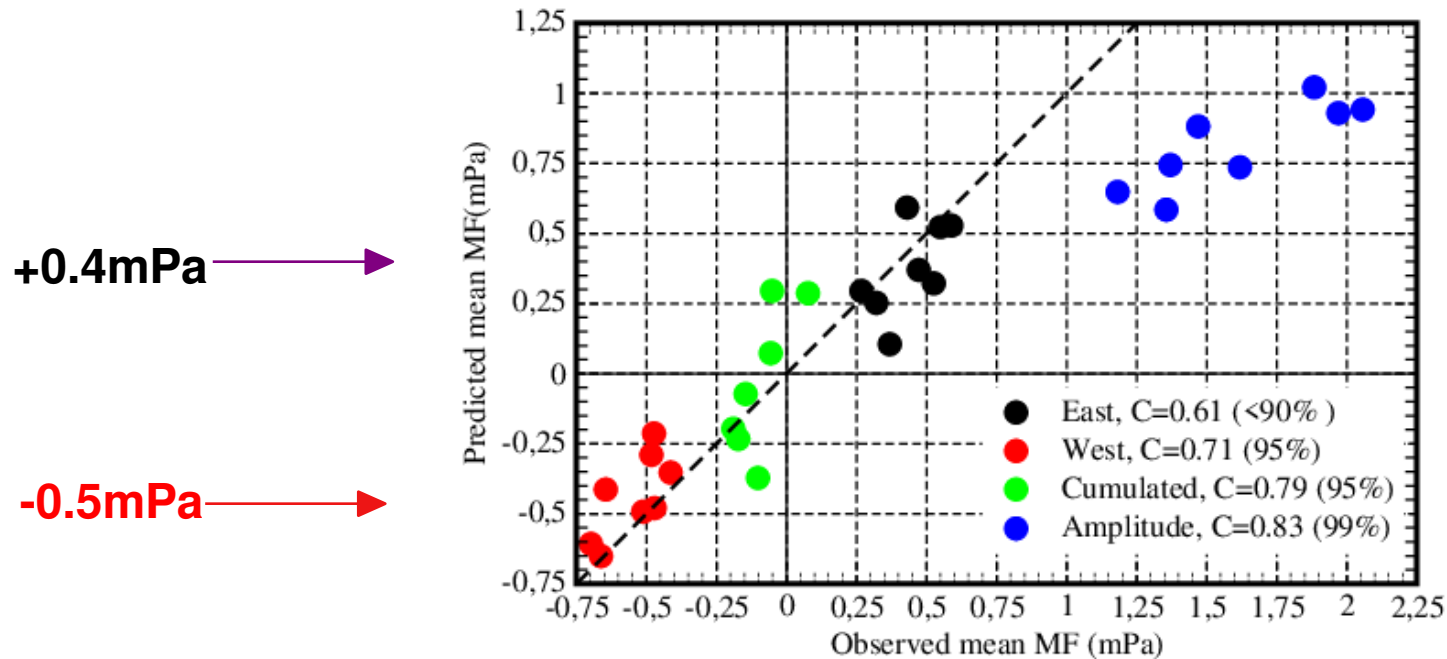
More flux when precipitation peaks

# Parameterization of GWs in large scale models

## 5) Validation against balloon observations

### Convective gravity waves and the tropics : Strateole 2

East and West MF averaged over the entire (8) balloon flights  
Offline predictions as function of observed momentum fluxes  
(15mn-1hr)



**We scientists are not fools !**



# Parameterization of GWs in large scale models

## 5) Validation against balloon observations

### Convective gravity waves and the tropics : Strateole 2

Correlation values daily data (“intraflight”),  
flight by flight

Flight	Altitude	Launch	End	Duration/DOF	Cumulated	Amplitude	East	West
01_STR1	20.7	12/11/2019	28/02/2020	107/53	0.23	<b>0.28</b>	<u><b>0.46</b></u>	<i>0.07</i>
02_STR2	20.2	11/11/2019	23/02/2020	103/51	<i>0.21</i>	<b>0.62</b>	<u><b>0.62</b></u>	<i>0.05</i>
03_TTL3	19.0	18/11/2019	28/02/2020	101/33	<u><b>0.49</b></u>	<b>0.42</b>	<u><b>0.49</b></u>	<b>0.43</b>
04_TTL1	18.8	27/11/2019	02/02/2020	67/22	<b>0.41</b>	<u><b>0.55</b></u>	<u><b>0.55</b></u>	<u><b>0.53</b></u>
05_TTL2	18.9	05/12/2019	23/02/2020	79/19	0.36	<i>0.29</i>	0.36	<i>0.24</i>
06_STR1	20.5	06/12/2019	01/02/2020	57/10	<i>0.39</i>	<b>0.67</b>	<u><b>0.71</b></u>	<b>0.59</b>
07_STR2	20.2	06/12/2019	28/02/2020	83/16	<i>0.01</i>	<i>0.09</i>	<i>0.08</i>	<i>0.06</i>
08_STR2	20.2	07/12/2019	22/02/2020	77/12	<i>0.18</i>	<u><b>0.7</b></u>	<u><b>0.66</b></u>	<i>0.37</i>
ALL	x	x	x	670/170	<u><b>0.30</b></u>	<u><b>0.41</b></u>	<u><b>0.51</b></u>	<u><b>0.29</b></u>

1-sided Pearson test according to the DOF and for each flight :

*<90*, *90-95*, **95-99**, **≥99**

# Parameterization of GWs in large scale models

## 5) Validation against balloon observations

### Quasi-Biennial Oscillation Initiative (QBOi) Models

Three standard non-orographic gravity waves (GWs) parameterizations tuned to produce a realistic tropical Quasi-Biennial Oscillation in 12 global climate models are used to predict in-situ balloon observations.

	Parameterization schemes	Climate Models
Global Spectral scheme	Warner and McIntyre (WMI)	CMAM, IFS, ECEarth, UMGA7gws
	Hines Doppler Spread (HDS)	ECham5, MIROC, MPIM, MRI-ESM, EMAC
	Multiwaves (Lindzen's type) <i>used relate GWs to their convective sources</i>	LMDz, HadGEM2, WACCM

# Parameterization of GWs in large scale models

## 5) Validation against balloon observations

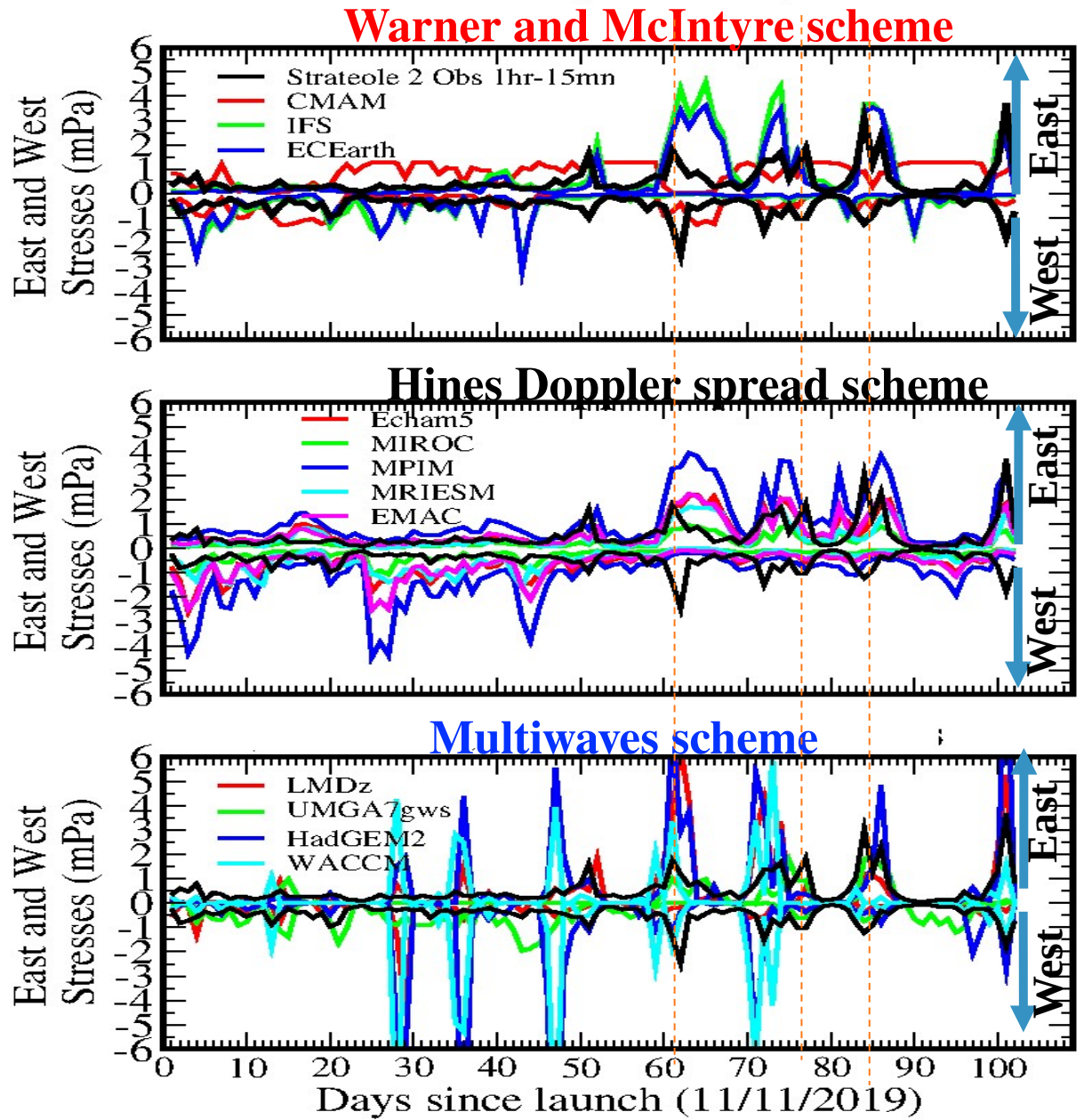
Quasi-Biennial Oscillation Initiative (QBOi) Models

Strateole 2 phase 1 flight 2

Predictions with the parameterizations using ERA5 data at the balloon location.

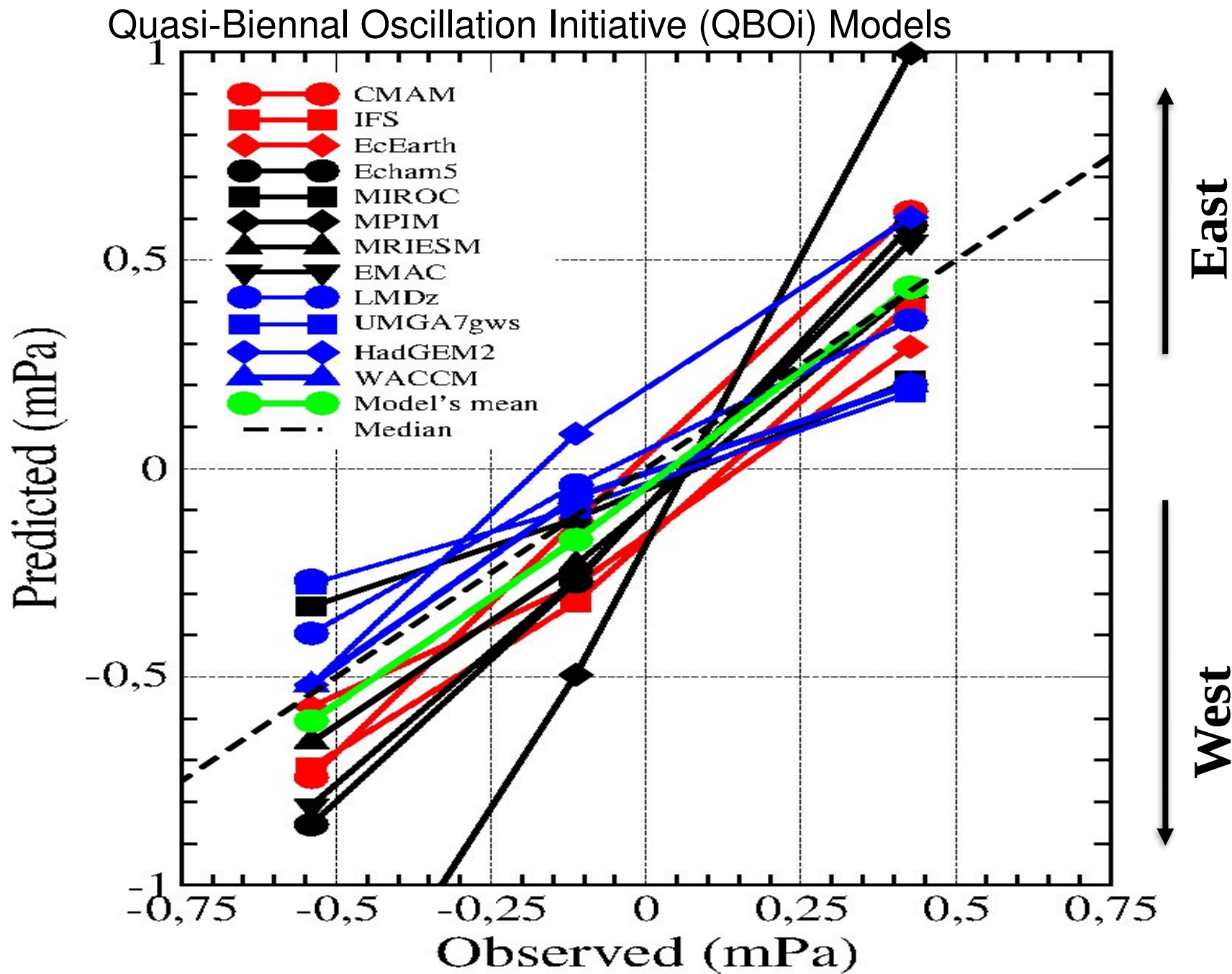
Large variety of behaviours, but some correspondance with **observation** in terms of amplitude.

More Flux when more precipitation near to **balloon** location (day 60, 75 and 83)



# Parameterization of GWs in large scale models

## 5) Validation against balloon observations

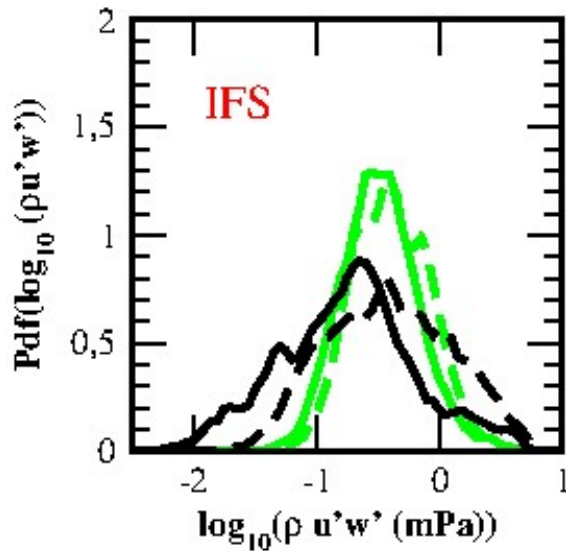


# Parameterization of GWs in large scale models

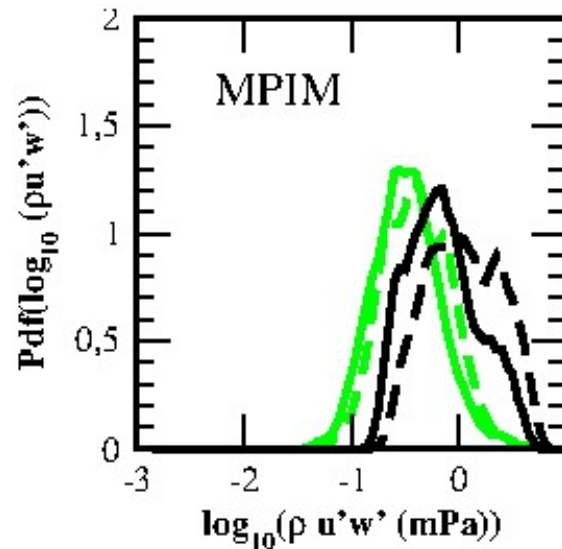
## 5) Validation against balloon observations

Quasi-Biennial Oscillation Initiative (QBOi) Models

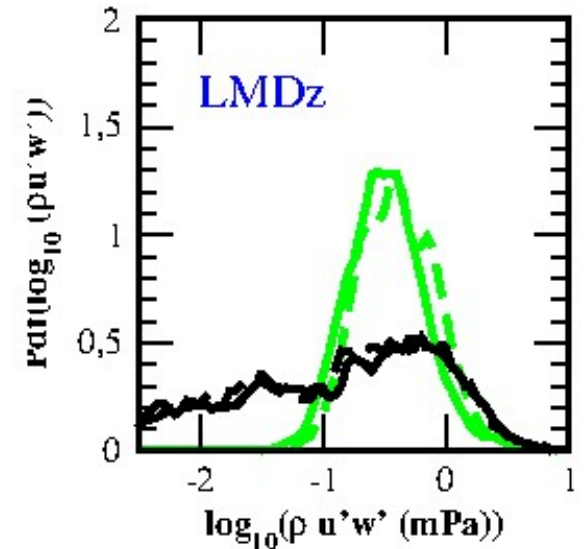
**Warner and McIntyre  
scheme**



**Hines Doppler spread  
scheme**



**Multiwaves  
scheme**



**Observation are in green and predictions are in black.**  
**Solid lines are for eastward and dashed lines are for westward.**



# Parameterization of GWs in large scale models

## 6) Perspectives

### Take home message:

« We scientific are not fool »

Good example of theories verified by obs a posteriori

### Perspective in terms of validation:

BAYESIAN estimate of parameters, including EnKF techniques?

Extent to Loon balloons

Extent to other GWs parameterization (frontal waves and mountain GWs)

Do improved schemes reduce model errors ?

Model tuning using uncertainty quantification (UQ)

Use of high resolution simul.s (DYAMON)

Use of Satellite observations that detect a fraction of the GW spectra (more global but coarser in resolution)

### In terms of dynamics :

Interaction between the boudary layer and mountain gravity waves

