

# Bibliographie du cours “Stabilité des écoulements parallèles”

Th. Gallay, 1er juin 2021

## I : Quelques références historiques et autres monographies

- [1] Lord Rayleigh, On the Stability, or Instability, of certain Fluid Motions, Proc. Lond. Math. Soc. **11** (1879/1880), 57–70.
- [2] O. Reynolds, An experimental investigation of the circumstances which determine whether the motion of water shall be direct or sinuous, and of the law of resistance in parallel channels, Phil. Trans. Roy. Soc. A **174** (1883), 935–982.
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## II : Écoulements parallèles plans

### A : cas non visqueux (Euler)

#### A1 : écoulement de Couette

- [13] Zhiwu Lin and Chongchun Zeng, Inviscid dynamical structures near Couette flow, ARMA **200** (2011), 1075–1097.
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- [17] A. Ionescu and Hao Jia, Inviscid damping near shear flows in a channel, CMP **374** (2020), 2015–2096.
- [18] M. Dolce, Nonlinear inviscid damping for zero mean perturbation of the 2D Euler Couette flow, preprint arXiv:1903.01543.
- [19] Yu Deng and Ch. Zillinger, Echo Chains as a Linear Mechanism: Norm Inflation, Modified Exponents and Asymptotics, preprint arXiv:1910.12914.

#### A2 : écoulements monotones plus généraux

- [20] Ch. Zillinger, Linear inviscid damping for monotone shear flows in a finite periodic channel, boundary effects, blow-up and critical Sobolev regularity, ARMA **221** (2016), 1449–1509.
- [21] Ch. Zillinger, Linear inviscid damping for monotone shear flows, Trans. Amer. Math. Soc. **369** (2017), 8799–8855.
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**A3 :** écoulements non monotones (dont Poiseuille et Kolmogorov)

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- [30] Zhiwu Lin and Chongchun Zeng, Unstable Manifolds of Euler Equations, *CPAM* **66** (2013), 1803–1836.
- [31] Dongyi Wei, Zhifei Zhang, and Weiren Zhao, Linear inviscid damping and vorticity depletion for shear flows, *Annals of PDE* **5** (2019), article 3, 101 p.

**B : Cas visqueux (Navier-Stokes)**

**B1 :** scalaires passifs

- [32] P. Constantin, A. Kiselev, L. Ryzhik, and A. Zlatoš, Diffusion and mixing in fluid flow, *Ann. Math.* **168** (2008), 643–674.
- [33] J. Bedrossian and M. Coti Zelati, Enhanced dissipation, hypoellipticity, and anomalous small noise inviscid limits in shear flows, *ARMA* **224** (2017), 1161–1204.
- [34] M. Coti Zelati, M. Delgadino, and T. Elgindi, On the relation between enhanced dissipation time-scales and mixing rates, *CPAM* **73** (2020), 1205–1244.
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- [36] M. Coti Zelati, Stable mixing estimates in the infinite Péclet number limit, *J. Functional Analysis* **279** (2020), 108562.
- [37] M. Coti Zelati and T.D. Drivas, A stochastic approach to enhanced diffusion, to appear in *Annali della Scuola Normale Superiore di Pisa* (2020).
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**B2 :** écoulement de Couette

- [41] J. Bedrossian, N. Masmoudi, and V. Vicol, Enhanced dissipation and inviscid damping in the inviscid limit of the Navier-Stokes equations near the two dimensional Couette flow, *ARMA* **219** (2016), 1087–1159.
- [42] J. Bedrossian, V. Vicol, and Fei Wang, The Sobolev stability threshold for 2D shear flows near Couette, *J. Nonlinear Sci.* **28** (2018), 2051–2075.
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**B3 :** écoulements plus généraux (NS linéarisé, ou NS complet)

- [46] M. Beck and C. E. Wayne, Metastability and rapid convergence to quasi-stationary bar states for the two-dimensional Navier-Stokes equations, *Proc. Roy. Soc. Edinburgh Sect. A* **143** (2013), 905–927.
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- [50] E. Grenier, T. Nguyen, F. Rousset, and A. Soffer, Linear inviscid damping and enhanced viscous dissipation of shear flows by using the conjugate operator method, *J. of Functional Analysis* **278** (2020), 108339.
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#### B4 : écoulements en présence de bords

- [53] Charles Li and Zhiwu Lin, A resolution of the Sommerfeld paradox, *SIAM J. Math. Anal.* **43** (2011), 1923–1954.
- [54] E. Grenier, Yan Guo, and Toan Nguyen, Spectral instability of characteristic boundary layer flows, *Duke Math. J.* **165** (2016), 3085–3146.
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### III : tourbillons plans

#### C : cas non visqueux (Euler)

- [67] Ch. Zillinger, On circular flows: linear stability and damping, *JDE* **263** (2017), 7856–7899.
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#### D : cas visqueux (Navier-Stokes)

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#### **IV : écoulements parallèles 3D**

- [74] J. Bedrossian, P. Germain, and N. Masmoudi, On the stability threshold for the 3D Couette flow in Sobolev regularity, *Ann. of Math.* **185** (2017), 541–608.
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ARMA = Archive for Rational Mechanics and Analysis

CMP = Communications in Mathematical Physics

CPAM = Communications in Pure and Applied Mathematics

CPDE = Communications in Partial Differential Equations

JDE = Journal of Differential Equations

JMFM = Journal of Mathematical Fluid Mechanics