

# A general extension theorem for cohomology classes on non reduced analytic spaces: dedicated to the memory of Professor Qikeng Lu

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**Abstract** : The main purpose of this paper is to generalize the celebrated  $L^2$  extension theorem of Ohsawa-Takegoshi in several directions : the holomorphic sections to extend are taken in a possibly singular hermitian line bundle, the subvariety from which the extension is performed may be non reduced, the ambient manifold is Kähler and holomorphically convex, but not necessarily compact.

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